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TECHNICAL NOTE 2878

COMBINED EFFECT OF DAMPING SCREENS AND STREAM

CONVERGENCE ON TURBULENCE

By Maurice Tucker

Lewis Flight Propulsion Laboratory Cleveland, Ohio

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TECHNICAL NOTE 2878

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By Maurice Tucker

SUMMARY

An analysis is presented of the combined effect of a series of damping screens followed by an axisymmetric-stream convergence (or divergence) upon the mean-square fluctuation-velocity intensities, scales, correlations, and one-dimensional spectra of a turbulence field convected by a main stream. The treatment is restricted to negligible turbulence decay and linearized by postulating small fluctuation velocities and velocity gradients, and absence of viscosity except as simulated by the idealized screen action. Compressibility of the main stream is allowed for during passage through the contracting section. The density fluctuations associated with the turbulence field are regarded as negligible.

Numerical results for the statistical quantities describing the turbulence field downstream of a screen-contraction configuration are obtained for the case of upstream isotropic turbulence. The action of the damping screens and the stream convergence is to distort this initially isotropic field into a field of turbulence symmetric about the longitudinal direction with the lateral fluctuation velocities greater in magnitude than the longitudinal velocities.

An approximate method of taking into account the effects of turbulence decay upon the mean-square fluctuation velocities obtained for the case of negligible decay is presented. This method of correction together with the tabulation of fluctuation-velocity ratios over an extensive range of conditions should prove useful for engineering applications.

INTRODUCTION

The use of fine-mesh or damping screens located in a low-speed settling chamber followed by a contracting passage (entrance cone) to attain a low-turbulence test-section flow is well known from the

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qualitative standpoint. Dryden and Schubauer (reference 1) have presented experimental data regarding the combined effect of screens and a contraction on the intensity of turbulence. Existing theoretical studies are confined to either the effect of the screens or of the stream contraction on turbulence. Taylor and Batchelor (reference 2) have obtained the effect of a damping screen located in a constant-area passage upon a triple Fourier integral representation of a turbulent field. The effect of a contraction upon a similar representation is analyzed in reference 3. In both references 2 and 3 initial isotropy is postulated in order to obtain numerical results.

The analyses of references 2 and 3 indicate that in the absence of decay effects (dissipation and mixing) an initially isotropic turbulence field will be distorted into a field of turbulence axisymmetric about the mean flow direction upon passage through either a damping screen or an axisymmetric contraction (contraction with all cross sections similar). An analysis of axisymmetric turbulence is given in reference 4. In conventional wind-tunnel configurations, turbulence that is initially isotropic will thus have been distorted into axisymmetric turbulence after passage through the first of the several damping screens and will remain axisymmetric while traversing the remaining screens and the following contraction. Inasmuch as the expressions obtained in reference 3 for the downstream mean-square velocity fluctuations require that the turbulence upstream of the contraction be isotropic, the results of references 2 and 3 cannot be combined in any simple manner to obtain the joint effect of screens and a contraction on turbulence that is initially isotropic.

The present analysis treats the combined effect of a series of N (symbols are defined in appendix A) identical damping screens and a downstream axisymmetric contraction upon the longitudinal and lateral turbulence velocity fluctuations, scales, correlations, and spectra of a turbulence field described by a triple Fourier integral. The configuration is shown schematically in figure 1. Although compressibility of the main stream is allowed for during passage through the contraction, the density fluctuations associated with the turbulence are regarded as negligible. The assumption of small turbulent velocity fluctuations and velocity gradients together with the postulated absence of viscosity, as in references 2 and 3, implies the absence of turbulent decay processes and linearizes the governing equations for both the screen and contraction effects.

After a discussion of the spectrum concepts used in the present analysis, the preliminary portions of the analysis which borrow from the results of references 2 and 3 are concerned with the effect of a screen and of a stream contraction upon a representative wave or Fourier component. Briefly, the screen affects only the amplitude vector of the wave; the contraction acts to change both the amplitude and wave-number

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vectors. In view of the linearized analysis and the resulting absence of modulation or mutual interference between the array of plane waves making up a field of turbulence, the correlation tensor is developed from the results obtained for a typical wave. The spectral tensor is obtained as the Fourier transform of the correlation tensor. Turbulence velocity and scale ratios obtained from the spectral densities (diagonal components of the spectral tensor) are then given in tabular form for the condition of upstream isotropic turbulence. The one-dimensional spectra and the correlation-coefficient curves for a special case of upstream isotropic turbulence are also determined. An approximation for taking into account decay effects is suggested. This investigation was conducted at the NACA Lewis laboratory.

ANALYSIS FOR NEGLIGIBLE DECAY

Spectral Representation of Turbulence

Turbulence is often regarded as an assembly of eddies of randomly varying size and intensity. The present analysis treats the turbulent field as a spectrum of plane sinusoidal waves with all possible wavelengths, wave-front orientations, and phases. This superposition provides the necessary three-dimensional character to the turbulence representation. Large eddies thus are represented by waves of large wavelength (small wave number). The fluctuation-velocity components $q_{\gamma}(\gamma=1,2,3)$ are represented at a given instant by the triple Fourier integral

$$q_{\gamma}(\underline{x}) = \iiint_{-\infty}^{\infty} Q_{\gamma}(\underline{k}) e^{i\underline{k}\cdot\underline{x}} dk_1 dk_2 dk_3$$
 (1)

where \underline{x} is a position vector, Q_{γ} a wave-amplitude vector (reference 3), and \underline{k} a wave-number vector normal to the wave front. In order that the wave amplitude vector Q_{γ} be finite, the field of turbulence described by equation (1) is assumed to occupy a bounded region and to vanish everywhere outside this region. For the case treated herein in which the fluctuation components are related by the incompressible-flow form of the continuity equation

$$\sum_{\Upsilon} Q_{\Upsilon} k_{\Upsilon} = 0 \tag{2}$$

the plane waves of equation (1) are transverse. In the summation of equation (2) the index γ covers the range of values 1, 2, 3.

In order to obtain the spectral tensor and, in turn, the mean-square velocity fluctuations, it will be convenient to discuss first the correlation tensor and indicate its relation with the spectral tensor. The correlation tensor $R_{\gamma\delta}(\underline{r})$ is defined as the spatial mean value of the product of the velocity component q_{γ} at \underline{x} and the velocity component q_{δ} at $\underline{x}'=\underline{x}+\underline{r}$ as \underline{x} varies and the separation vector \underline{r} of the two points remains fixed during the averaging. If it is assumed that the field of turbulence is homogeneous and statistically steady and that the field is confined to a parallelepiped of edges $2D_1,\ 2D_2,\ 2D_3$ and vanishes everywhere outside, the space average is derived in reference 3 as

$$R_{\gamma\delta}(\underline{\mathbf{r}}) = \lim_{\tau \to \infty} \iiint_{-\infty}^{\infty} \frac{8\pi^3}{\tau} Q_{\gamma}(\underline{\mathbf{k}}) Q_{\delta}^{*}(\underline{\mathbf{k}}) e^{-i\underline{\mathbf{k}}\cdot\underline{\mathbf{r}}} dk_1 dk_2 dk_3$$

where $Q_{\delta}^*(\underline{k})$ is the complex conjugate of $Q_{\delta}(\underline{k})$ and $\underline{\tau}$ is the volume $8D_1D_2D_3$ of the parallelepiped. The expression $\lim_{\substack{\tau \to \infty}} \frac{8\pi^3}{\tau} Q_{\gamma}(\underline{k})Q_{\delta}^*(\underline{k})$ is equivalent to the spectral tensor $\Gamma_{\gamma\delta}(\underline{k})$ defined in reference 5 as the Fourier transform of the correlation tensor $R_{\gamma\delta}(\underline{r})$

$$R_{\gamma\delta}(\underline{r}) = \iiint_{\infty} \Gamma_{\gamma\delta}(\underline{k}) e^{-i\underline{k}\cdot\underline{r}} dk_1 dk_2 dk_3$$

or

$$\Gamma_{\gamma\delta}(\underline{k}) = \lim_{T \to \infty} \frac{8\pi^3}{T} Q_{\gamma}(\underline{k}) Q_{\delta}^*(\underline{k})$$
 (3)

A knowledge of the spectral tensor permits, as will be shown, determination of the various statistical quantities describing a turbulence field. Equation (3), which relates the spectral tensor to the waveamplitude vector obtained for a typical Fourier component in the absence of any modulation effects, is thus basic to the present analysis.

For isotropic homogeneous turbulence fields wherein the incompressible flow form of the continuity equation is satisfied, Batchelor (reference 5) has shown that the spectral tensor can be written

$$\Gamma_{\gamma\delta}(\underline{k}) = G(k) \left(k^2 \delta_{\gamma\delta} - k_{\gamma} k_{\delta} \right)$$
 (4a)

where $k^2 \equiv k_1^2 + k_2^2 + k_3^2$, $\delta_{\gamma\delta} = 1$ for $\gamma = \delta$, and $\delta_{\gamma\delta} = 0$ for $\gamma \neq \delta$.

In matrix form

$$\Gamma_{\gamma\delta}(\underline{k}) = G(k) \begin{vmatrix} k_2^2 + k_3^2 & -k_1k_2 & -k_1k_3 \\ -k_1k_2 & k_1^2 + k_3^2 & -k_2k_3 \\ -k_1k_3 & -k_2k_3 & k_1^2 + k_2^2 \end{vmatrix}$$
(4b)

It is clear from the definition of the correlation tensor that for $\underline{r} = 0$ the diagonal elements of the tensor yield the mean-square velocity fluctuations. In terms of the corresponding elements of the spectral tensor (energy spectral densities)

$$\frac{1}{q_{\gamma}^{2}} = \iiint_{-\infty}^{\infty} \Gamma_{\gamma\gamma}(\underline{k}) dk_{1}dk_{2}dk_{3}$$
 (5)

The mean-square velocity fluctuations of equation (5) refer to spatial averages. Hot-wire instrumentation used to obtain these fluctuations, however, provides only time averages. Taylor (reference 6) was able to show that the spectrum of the velocity fluctuations in time is the Fourier transform of the spatial correlation function. Taylor's hypothesis (reference 7) that the main stream carries along the pattern of a weak field of turbulence unchanged past the point of measurement permits analysis of the hot-wire output signal in the form of a one-dimensional spectrum defined in the equivalent of spatial terms. The relation between the one-dimensional spectral densities F_{γ} and the three-dimensional spectral densities $\Gamma_{\gamma\gamma}$ is easily shown by writing equation (5) as

$$\frac{1}{q_{\gamma}^{2}} = \int_{0}^{\infty} \left[\int_{-\infty}^{\infty} \mathbf{r}_{\gamma\gamma}(\underline{\mathbf{k}}) \, d\mathbf{k}_{2} d\mathbf{k}_{3} \right] d\mathbf{k}_{1} \equiv \int_{0}^{\infty} \mathbf{r}_{\gamma}(\mathbf{k}_{1}) \, d\mathbf{k}_{1}$$
 (6)

The various statistical quantities which characterize a field of turbulence may be obtained from the one-dimensional spectral densities

as discussed in reference 8. Noting that $\frac{1}{q_{\gamma}^2} \int_0^{\infty} F_{\gamma}(k_1) dk_1 = 1$, the correlation coefficients are given by

$$R_{\gamma}(r_{1}) \equiv \frac{R_{\gamma\gamma}(r_{1},0,0)}{\overline{q_{\gamma}^{2}}} = \frac{1}{\overline{q_{\gamma}^{2}}} \int_{0}^{\infty} F_{\gamma}(k_{1}) \cos k_{1}r_{1} dk_{1}$$
 (7)

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The Fourier transform relations yield

$$F_{\gamma}(k_{1}) = \frac{2\overline{q_{\gamma}^{2}}}{\pi} \int_{0}^{\infty} R_{\gamma} \cos k_{1}r_{1} dr_{1}$$
 (8)

Two sets of characteristic lengths are customarily defined for a turbulence field. The turbulence microscales λ_{γ} (mean lengths weighted in favor of the small eddies which are responsible for the greater part of the viscous dissipation) are given by

$$\frac{1}{\lambda_{\gamma}^{2}} = -\left(\frac{\partial^{2} R_{\gamma}}{\partial r_{1}^{2}}\right)_{r_{1}=0} = \frac{1}{q_{\gamma}^{2}} \int_{0}^{\infty} k_{1}^{2} F_{\gamma}(k_{1}) dk_{1}$$
 (9)

The turbulence scales I_{γ} (mean lengths representative of the average size of all the eddies) are obtained as

$$L_{\gamma} \equiv \int_{0}^{\infty} R_{\gamma} dr_{1} = \frac{\pi}{2q_{\gamma}^{2}} \left[F_{\gamma}(k_{1}) \right]_{k_{1}=0}$$
 (10)

This physical meaning for the scale of turbulence is only applicable when $R_{\gamma}>0$ as $r_1\to\infty.$

Plane-Wave Analysis for Damping Screens

The preceding equations indicate that the statistical quantities describing a field of turbulence may be obtained from the spectral tensor of equation (3), which is presented in terms of the plane-wave amplitude vectors $Q_{\gamma}(\underline{k})$. The assumptions of small turbulent velocity fluctuations and of inviscid flow, with regard to both the main stream and the turbulence field convected by the main stream, linearize the equations which govern the action of the screens and of the contraction. In the resulting absence of any modulation or interaction effects between waves, the analysis is simplified by first treating the effect of a screen and a stream convergence (or divergence) upon a representative plane wave. Superposition is then used to obtain the combination of these effects upon the complete assembly of plane waves which describes the turbulent field.

The action of a fine-mesh or damping screen on a disturbance convected by a low-speed uniform stream may be characterized by two parameters K and $\alpha.$ The parameter K is defined in terms of the pressure drop ΔP required to drive fluid of density ρ and velocity U through the screen

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$$K \equiv \Delta P / \frac{1}{2} \rho U^2$$

The parameter α which takes into account the side force per unit area was introduced by Taylor in reference 9 and relates the angles of flow incidence ψ_1 and flow emergence ψ_2 shown in figure 2. It has been shown experimentally that the ratio $\tan \psi_2/\tan \psi_1$ tends to a finite limit α as ψ_1 , which is usually very small, tends toward zero. For incompressible flow the continuity equation requires that the longitudinal velocity component be unchanged after passage through the screen. From kinematical considerations, at the screen the ratio of downstream to upstream lateral velocity components equals α for small values of the flow incidence angle ψ_1 .

As in reference 2 the uniform stream is regarded as incompressible and inviscid throughout the constant-area settling chamber in which the screens are located (station A to station B of fig. 1). A screen will, in general, decrease turbulent motions of larger scale than the mesh size and introduce turbulence of smaller scale. In the analysis the damping screens are assumed not to generate any wake turbulence, which implies that the screen mesh size and wire diameter are very small relative to the scale of the upstream turbulence. Far upstream of the screen, at station A, a single plane wave carried along by the main stream of velocity U in the x_1 -direction will be designated

$$\tilde{\mathbf{q}}_{\mathbf{r}}^{A} = \tilde{\mathbf{Q}}_{\mathbf{r}}^{A} e^{i(\underline{\mathbf{k}} \cdot \underline{\mathbf{x}} - \mathbf{k}_{1} \mathbf{U} \mathbf{t})}$$

Coordinate axes are fixed, with the origin located at the screen and the positive x_1 -axis pointing downstream. It is shown in reference 2 on the basis of a steady-state disturbance analysis that far downstream of the screen, at station B, the wave is transformed to

$$\tilde{\mathbf{q}}_{\mathbf{Y}}^{B} = \tilde{\mathbf{Q}}_{\mathbf{Y}}^{B} e^{i(\underline{\mathbf{k}} \cdot \underline{\mathbf{x}} - \mathbf{k}_{\underline{\mathbf{I}}} \mathbf{U} \mathbf{t})}$$

In order to satisfy conditions at the screen, it is necessary to postulate disturbance fields upstream and downstream of the screen which are induced by the screen. These disturbance fields attenuate, vanishing at stations A and B. Taylor and Batchelor represent these induced velocities in terms of potential flows. With the velocity components u, v, w of figure 2 designating the combined effect of the turbulent velocity fluctuations and the induced velocities, the following conditions are imposed at the screen $(x_1 = 0)$

$$(u)_{x_1=0}^B = (u)_{x_1=0}^A$$

The root-mean-square fluctuation velocities are taken to be small relative to the stream velocity so that the equations of motion can be linearized. A further condition is imposed that the local pressure drop across the screen is determined by the local longitudinal velocity and the screen pressure-drop coefficient K. The basic relations describing this idealized action of a damping screen on a representative plane wave are then obtained in reference 2 as

$$\tilde{\mathbf{Q}}_{1}^{B} = \tilde{\mathbf{Q}}_{1}^{A} \frac{(\beta+i)(2\alpha\beta-i\boldsymbol{v})}{(\beta-i)(2\beta+i\mu)}$$
 (11a)

$$\tilde{\mathbf{Q}}_{2}^{B} = \alpha \tilde{\mathbf{Q}}_{2}^{A} + \frac{i\tilde{\mathbf{Q}}_{1}^{A} k_{1} k_{2}}{\zeta^{2}} \left[\frac{\beta(\alpha-1)^{2} + i(\boldsymbol{v} - \alpha \mu)}{(\beta-i)(2\beta + i\mu)} \right]$$
 (11b)

$$\tilde{\mathbf{Q}}_{3}^{B} = \alpha \tilde{\mathbf{Q}}_{3}^{A} + \frac{i\tilde{\mathbf{Q}}_{1}^{A} \mathbf{k}_{1} \mathbf{k}_{3}}{\zeta^{2}} \left[\frac{\beta(\alpha-1)^{2} + i(\mathbf{v} - \alpha\mu)}{(\beta-i)(2\beta+i\mu)} \right]$$
(11c)

where
$$\zeta^2 \equiv k_2^2 + k_3^2$$
, $\beta^2 \equiv \frac{k_1^2}{\zeta^2}$, $\mu \equiv (1+\alpha+K)$, and $\nu \equiv (1+\alpha-\alpha K)$.

Plane-Wave Analysis for Contraction Section

The main stream will be regarded as compressible and inviscid throughout the contraction section (station B to station C of fig. 1). In the case of supersonic test-section flow, the term "contraction" is retained for convenience. As before, the turbulent field is taken to be incompressible and inviscid. The contraction section has its initial breadth and height reduced by the factors l_2 and l_3 , respectively, while the velocity $U(x_1)$ at station B is increased to $l_1U(x_1)$ at station C. A cubical fluid volume element of edge D at station B will have been distorted into a parallelepiped of edges l_1D , l_2D , l_3D upon reaching station C (fig. 3). The effect of a contraction upon a turbulent field arises principally from changes in vorticity following such distortion of the fluid elements passing through the contraction.

At station B (time t=0) in figure 3, a particle at distance \underline{x} from a corner particle of a given fluid element will at station C (time t=t) be at a distance \underline{x} from the corner particle. The coordinate axes are taken to move with the main stream at velocity $U(x_1)$. With the assumption of a weak turbulence field, the relative displacement of adjacent particles in a given fluid element due to turbulent

mixing is taken to be very much smaller than the displacement due to the contraction. The relation between x and χ is then simply

$$\chi_{\gamma} = l_{\gamma} x_{\gamma} \tag{12}$$

With equation (12) the continuity equation for the main stream in Lagrangean form provides the relation

$$\sigma l_1 l_2 l_3 = 1$$
 (13)

where σ is the ratio of stream density at station C to stream density at station B. The product l_2l_3 represents the ratio of tunnel cross-sectional area at station C to tunnel area at station B. The parameter l_1 represents the speed ratio referred to these stations.

The equations describing the changes in vorticity following distortion of a fluid element are, from reference 9:

$$\alpha^{\lambda}_{C} = \alpha \sum_{Q} \alpha^{Q}_{Q} \frac{9x^{Q}}{9x^{\lambda}}$$

Use of equation (12) linearizes these equations relating the upstream and downstream vorticities to

$$\omega_{\Upsilon}^{C} = \sigma l_{\Upsilon} \omega_{\Upsilon}^{B} \tag{14}$$

Upstream of the contraction at station B, a single plane wave being carried along by the main stream is designated at time t=0 by

$$\tilde{\mathbf{q}}_{\mathbf{Y}}^{\mathbf{B}} = \tilde{\mathbf{Q}}_{\mathbf{Y}}^{\mathbf{B}} e^{i\underline{\mathbf{k}}\cdot\underline{\mathbf{x}}}$$
 (15)

The vorticity at station B is obtained from the curl of equation (15). A velocity distribution at station C compatible with equation (14) and satisfying continuity, equation (2), is obtained in reference 3 as

$$\tilde{\mathbf{q}}_{\mathbf{r}}^{C} = \tilde{\mathbf{Q}}_{\mathbf{r}}^{C} e^{i\mathbf{\kappa}\cdot\mathbf{X}}$$

where the wave-amplitude vector is

$$\tilde{\mathbf{Q}}_{\gamma}^{C} = \frac{1}{l\gamma} \left(\tilde{\mathbf{Q}}_{\gamma}^{B} - \sum_{\delta} \frac{\tilde{\mathbf{Q}}_{\delta}^{B} \mathbf{k}_{\delta} \mathbf{k}_{\gamma}}{l_{\delta}^{2} \mathbf{k}^{2}} \right)$$
(16)

and where the new wave-number vector resulting from distortion of the fluid volume element is given by

$$\underline{\kappa} = \frac{k_1}{l_1}, \frac{k_2}{l_2}, \frac{k_3}{l_3} \tag{17}$$

Thus both the wave-number and wave-amplitude vectors of a plane wave are altered in going through a contraction, whereas only the amplitude vector is altered in traversing a screen.

Equations (16) and (17) describe the effect of an arbitrary contraction on a representative plane wave. For an axisymmetric contraction defined by the condition $l_2 = l_3$ (all cross sections are similar but not necessarily circular), equation (16) with the aid of equation (2) simplifies, in expanded form, to

$$\tilde{\mathbf{Q}}_{1}^{C} = \frac{\tilde{\mathbf{Q}}_{1}^{B}}{l_{1}} \frac{\mathbf{k}_{1}^{2} + \zeta^{2}}{\boldsymbol{\epsilon} \, \mathbf{k}_{1}^{2} + \zeta^{2}} \tag{18a}$$

$$\tilde{\mathbf{Q}}_{2}^{C} = \frac{1}{l_{2}} \left[\tilde{\mathbf{Q}}_{2}^{B} + \frac{\tilde{\mathbf{Q}}_{1}^{B} \mathbf{k}_{1} \mathbf{k}_{2} (1 - \epsilon)}{\epsilon \mathbf{k}_{1}^{2} + \zeta^{2}} \right]$$
 (18b)

$$\tilde{\mathbf{Q}}_{3}^{C} = \frac{1}{l_{2}} \left[\tilde{\mathbf{Q}}_{3}^{B} + \frac{\tilde{\mathbf{Q}}_{1}^{B} \mathbf{k}_{1} \mathbf{k}_{3} (1 - \epsilon)}{\epsilon \, \mathbf{k}_{1}^{Z} + \zeta^{2}} \right]$$
(18c)

where $\epsilon \equiv {l_2}^2/{l_1}^2$. For an axisymmetric contraction, the contraction parameters l_1 , l_2 , and ϵ may be expressed in terms of the Mach numbers at stations B and C as follows:

$$l_1^2 = \left(\frac{M_C}{M_B}\right)^2 \left(\frac{5 + M_B^2}{5 + M_C^2}\right)$$

$$l_2^2 = \left(\frac{M_B}{M_C}\right) \left(\frac{5 + M_C^2}{5 + M_B^2}\right)^3$$

$$\epsilon = \left(\frac{M_B}{M_C}\right)^3 \left(\frac{5 + M_C^2}{5 + M_B^2}\right)^4$$
(19)

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Spectral Tensors for Multiple-Screen-Contraction Configurations

Equations (11) and (18) describe the effect of a screen and an axisymmetric contraction $(l_2=l_3)$, respectively, upon the amplitude vector \tilde{Q}_{γ} of a single plane wave typical of the assembly of waves representing the turbulence field (equation (1)). In the Fourier integral \tilde{q}_{γ} corresponds to dq_{γ} , $\tilde{Q}_{\gamma}(k)$ to Q_{γ} $dk_1dk_2dk_3$, and $\tilde{Q}_{\gamma}(\underline{k})$ to Q_{γ} $dk_1dk_2dk_3$. Since at station C (fig. 1) the distortion resulting from the contraction transforms the wave-number vector from \underline{k} to \underline{k} and that for axisymmetry $dk_1dk_2dk_3 = l_1l_2^2 dk_1dk_2dk_3$, equations (11) and (18) yield

$$Q_1^B = Q_1^A \frac{(\beta+i)(2\alpha\beta-i\nu)}{(\beta-i)(2\beta+i\mu)}$$
 (20a)

$$Q_{2}^{B} = \alpha Q_{2}^{A} + \frac{iQ_{1}^{A}k_{1}k_{2}}{\zeta^{2}} \left[\frac{\beta(\alpha-1)^{2} + i(\nu - \alpha\mu)}{(\beta-i)(2\beta + i\mu)} \right]$$
 (20b)

$$Q_{3}^{B} = \alpha Q_{3}^{A} + \frac{iQ_{1}^{A}k_{1}k_{3}}{\zeta^{2}} \left[\frac{\beta(\alpha-1)^{2} + i(\nu - \alpha\mu)}{(\beta-i)(2\beta + i\mu)} \right]$$
(20c)

$$Q_1^C = l_2^2 Q_1^B \left(\frac{k_1^2 + \zeta^2}{\epsilon k_1^2 + \zeta^2} \right)$$
 (20d)

$$Q_2^{C} = l_1 l_2 \left[Q_2^{B} + \frac{Q_1^{B} k_1 k_2 (1 - \epsilon)}{\epsilon k_1^{2} + \zeta^{2}} \right]$$
 (20e)

$$Q_3^{C} = l_1 l_2 \left[Q_3^{B} + \frac{Q_1^{B} k_1 k_3 (1 - \epsilon)}{\epsilon k_1^{2} + \zeta^{2}} \right]$$
 (20f)

If the fluid element volume τ is taken to be a cube of edge D at station A, and hence at station B, the volume will have been distorted into a parallelepiped of edges $l_1 D$, $l_2 D$, $l_2 D$ at station C for an axisymmetric contraction. The energy spectral densities which enter directly into the calculation of turbulence fluctuation velocities are obtained from equation (3) as

$$\left[\Gamma_{\gamma\gamma}(\underline{k})\right]^{A,B} = \lim_{D \to \infty} \frac{8\pi^3}{D^3} \left[Q_{\gamma}(\underline{k})Q_{\gamma}^*(\underline{k})\right]^{A,B} \tag{21a}$$

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$$\left[\Gamma_{\gamma\gamma}(\underline{\kappa})\right]^{C} = \lim_{D \to \infty} \frac{8\pi^{3}}{l_{1}l_{2}^{2}D^{3}} \left[Q_{\gamma}(\underline{\kappa})Q_{\gamma}^{*}(\underline{\kappa})\right]^{C}$$
(21b)

With the products $Q_{\gamma}Q_{\gamma}^{*}$ from equations (20) formed and with the use of equations (21) and the continuity relations $Q_{\gamma}k_{\gamma}=0$ and $Q_{\gamma}^{*}k_{\gamma}=0$, the energy spectral densities may be written as:

$$\Gamma_{11}^{B}(\underline{k}) = \left(\frac{4\alpha^{2}k_{1}^{2} + \nu^{2}\zeta^{2}}{4k_{1}^{2} + \mu^{2}\zeta^{2}}\right)\Gamma_{11}^{A}(\underline{k})$$
 (22a)

$$\left[\Gamma_{22}(\underline{\mathbf{k}}) + \Gamma_{33}(\underline{\mathbf{k}})\right]^{B} = \alpha^{2}\left[\Gamma_{22}(\underline{\mathbf{k}}) + \Gamma_{33}(\underline{\mathbf{k}})\right]^{A} + \frac{(v^{2} - \alpha^{2}\mu^{2})k_{1}^{2}}{4k_{1}^{2} + \mu^{2}\zeta^{2}} \Gamma_{11}^{A}(\underline{\mathbf{k}})$$

$$\Gamma_{11}^{C}(\underline{\kappa}) = \frac{\iota_{2}^{2}}{\iota_{1}} \left(\frac{\kappa_{1}^{2} + \zeta^{2}}{\epsilon \kappa_{1}^{2} + \zeta^{2}}\right)^{2} \Gamma_{11}^{B}(\underline{\kappa})$$
 (22c)

$$\left[\mathbf{r}_{22}(\underline{\mathbf{k}}) + \mathbf{r}_{33}(\underline{\mathbf{k}})\right]^{C} = \imath_{1} \left\{ \left[\mathbf{r}_{22}(\underline{\mathbf{k}}) + \mathbf{r}_{33}(\underline{\mathbf{k}})\right]^{B} + \left[\frac{\mathbf{k}_{1}^{2}(1-\epsilon)^{2}\zeta^{2} - 2\mathbf{k}_{1}^{2}(1-\epsilon)(\epsilon\mathbf{k}_{1}^{2}+\zeta^{2})}{(\epsilon\mathbf{k}_{1}^{2}+\zeta^{2})^{2}}\right] \mathbf{r}_{11}^{B}(\underline{\mathbf{k}}) \right\}$$
(22d)

With the use of equations (22a) and (22c), the longitudinal energy spectral density at station C for N screens in series followed by an axisymmetric contraction may be expressed in terms of the spectral density at station A as

$$\left[\Gamma_{11}^{C}(\underline{\kappa})\right]_{N} = \frac{l_{2}^{2}}{l_{1}} \left(\frac{k_{1}^{2} + \zeta^{2}}{\epsilon k_{1}^{2} + \zeta^{2}}\right)^{2} \left(\frac{4\alpha^{2}k_{1}^{2} + v^{2}\zeta^{2}}{4k_{1}^{2} + \mu^{2}\zeta^{2}}\right)^{N} \left[\Gamma_{11}^{A}(\underline{k})\right]$$
(23)

For conciseness, equations (22a), (22b), and (22d) may be written as $\mathrm{H_1}^B = \Lambda \mathrm{H}^A$, $\mathrm{V_1}^B = \alpha^2 \mathrm{V_1}^A + \Sigma \mathrm{H}^A$, and $\mathrm{V_1}^C = l_1 \mathrm{V_1}^B + l_1 \Omega \mathrm{H_1}^B$, respectively. Then for N screens in series, $\mathrm{H_N}^B = \Lambda \mathrm{H_{N-1}^B} = \Lambda^N \mathrm{H}^A$, $\mathrm{V_N}^B = \alpha^2 \mathrm{V_{N-1}^B} + \Sigma \mathrm{H_{N-1}^B}$, and $\mathrm{V_N}^C = l_1 \mathrm{V_N}^B + l_1 \Omega \mathrm{H_N}^B$. The lateral energy spectral densities at station C for N screens in series followed by an axisymmetric contraction may then be grouped as

$$\left[\mathbf{r}_{22}^{\mathbf{C}}(\underline{\kappa}) + \mathbf{r}_{33}^{\mathbf{C}}(\underline{\kappa})\right]_{\mathbf{N}} = \alpha^{2}\left[\mathbf{r}_{22}^{\mathbf{C}}(\underline{\kappa}) + \mathbf{r}_{33}^{\mathbf{C}}(\underline{\kappa})\right]_{\mathbf{N}-1} + \frac{\imath_{1}(\nu^{2} - \alpha^{2}\mu^{2}) k_{1}^{2}}{4k_{1}^{2} + \mu^{2}\xi^{2}}\left[1 - \frac{(1-\epsilon)\xi^{2}}{\epsilon k_{1}^{2} + \xi^{2}}\right]^{2} \frac{4\alpha^{2}k_{1}^{2} + \nu^{2}\xi^{2}}{4k_{1}^{2} + \mu^{2}\xi^{2}}\right]^{\mathbf{N}-1} \left[\mathbf{r}_{11}^{\mathbf{A}}(\underline{k})\right]$$
(24)

Equations (23) and (24) relate the energy spectral densities downstream of a multiple-screen-axisymmetric-contraction configuration to the corresponding upstream spectral densities at station A.

Results for Negligible Decay

The solutions to be given (see appendixes B and C) will now be restricted to the case of isotropic upstream turbulence. The upstream energy spectral densities $\Gamma_{\gamma\gamma}^{\quad A}(\underline{k})$ may then be obtained from equations (4).

Turbulence velocity ratios. - As shown in appendix B, the turbulence velocity ratio or ratio of mean-square fluctuation velocities downstream of a series of N identical screens followed by an axisymmetric contraction to the corresponding upstream fluctuation velocities is given for initially isotropic turbulence by

$$\frac{\left(\overline{q_1^2}\right)_N^C}{\left(\overline{q_1^2}\right)^A} = \frac{3a^4}{4l_1^2} \int_0^{\pi} \frac{\Delta^N \sin^3 \theta \, d\theta}{\left(a^2 - \cos^2 \theta\right)^2} \tag{25}$$

$$\frac{\left(\frac{\overline{q_{2}^{2}}}{\sqrt{N}}\right)_{N}^{C}}{\left(\frac{\overline{q_{2}^{2}}}{\sqrt{N}}\right)_{N}^{A}} = \frac{\left(\frac{\overline{q_{2}^{2}}}{\sqrt{N}}\right)_{N-1}^{C}}{\left(\frac{\overline{q_{2}^{2}}}{\sqrt{N}}\right)_{N-1}^{A}} + \frac{3(a^{2}-1)^{2}(v^{2}-\alpha^{2}\mu^{2})}{8l_{2}^{2}} \int_{0}^{\pi} \frac{\Delta^{N-1}\sin^{3}\theta\cos^{2}\theta\,d\theta}{(4\cos^{2}\theta+\mu^{2}\sin^{2}\theta)(a^{2}-\cos^{2}\theta)^{2}}$$
(26)

where
$$a^2 = \frac{1}{1-\epsilon}$$
 and $\Delta = \frac{4\alpha^2 \cos^2 \theta + v^2 \sin^2 \theta}{4 \cos^2 \theta + u^2 \sin^2 \theta}$

A convenient approximation for equation (26) is presented later (see equation (39)).

For N = 1, equation (25) for the longitudinal turbulence velocity ratio integrates to

$$\frac{\left(\overline{q_{1}^{2}}\right)_{1}^{C}}{\left(\overline{q_{1}^{2}}\right)_{1}^{A}} = \frac{3a^{4}\eta^{2}v^{2}}{4l_{1}^{2}\mu^{2}\xi^{2}(a^{2}-\eta^{2})^{2}} \left[\frac{(a^{2}-\eta^{2})(\xi^{2}-a^{2})}{a^{2}} + A_{1}\left(\frac{1}{a} \tanh^{-1} \frac{1}{a}\right) + A_{2}\left(\frac{1}{\eta} \tanh^{-1} \frac{1}{\eta}\right)\right] \tag{27}$$

where

$$\xi^2 \equiv \frac{v^2}{v^2 - 4\alpha^2}$$

$$\eta^2 \equiv \frac{\mu^2}{\mu^2 - 4}$$

$$A_{1} \equiv a^{2}(a^{2}+1) + \eta^{2}(1-3a^{2}) + \frac{\xi^{2}[a^{2}-1)^{2} + (a^{2}+1)(\eta^{2}-1)]}{a^{2}}$$

$$A_{2} \equiv 2(\eta^{2}-1)(\eta^{2}-\xi^{2})$$

Equation (26) for the lateral velocity ratio (see appendix B) integrates for N = 1 to

$$\frac{\left(\overline{q_{2}^{2}}\right)_{1}^{C}}{\left(\overline{q_{2}^{2}}\right)^{A}} = \frac{\alpha^{2}}{l_{2}^{2}} + \frac{v^{2}\eta^{2}}{8l_{2}^{2}\xi^{2}\mu^{2}} \left[B_{1} + B_{2}\left(\frac{1}{a} \tanh^{-1} \frac{1}{a}\right) - B_{3}\left(\frac{1}{\eta} \tanh^{-1} \frac{1}{\eta}\right)\right]$$
(28)

where

$$\begin{split} \mathbf{B}_1 &\equiv \frac{\mu^2}{2\eta^2} \left(\boldsymbol{\xi}^2 - \eta^2 \right) (2 - 3\eta^2) + 6 (\boldsymbol{\xi}^2 - \eta^2) - 2 + \frac{3(\mathbf{a}^2 - 1)(\mathbf{a}^2 - \boldsymbol{\xi}^2)}{(\mathbf{a}^2 - \eta^2)} \\ \mathbf{B}_2 &\equiv \frac{3(\mathbf{a}^2 - 1)^2}{(\mathbf{a}^2 - \eta^2)^2} \left[\mathbf{a}^2 (3\eta^2 - \mathbf{a}^2) - \boldsymbol{\xi}^2 (\mathbf{a}^2 + \eta^2) \right] \\ \mathbf{B}_3 &\equiv \frac{3(\eta^2 - 1)(\boldsymbol{\xi}^2 - \eta^2)}{2} \left[(4 - \mu^2) - \frac{4(\mathbf{a}^4 - \eta^2)}{(\mathbf{a}^2 - \eta^2)^2} \right] \end{split}$$

For the case of axisymmetric contraction with the screen absent (α^2 =1, K \rightarrow 0), equations (27) and (28) reduce, respectively, to

$$\frac{\left(\overline{q_{1}^{2}}\right)_{0}^{C}}{\left(q_{1}^{2}\right)_{A}^{A}} = \frac{\left(\overline{q_{1}^{2}}\right)_{0}^{C}}{\left(q_{1}^{2}\right)_{B}^{B}} = -\frac{3a^{2}}{4l_{1}^{2}}\left[1 - (a^{2}+1)\left(\frac{1}{a} \tanh^{-1} \frac{1}{a}\right)\right]$$

and

$$\frac{\left(\overline{q_2^2}\right)_0^C}{\left(q_2^2\right)_A^A} = \frac{\left(\overline{q_2^2}\right)_0^C}{\left(q_2^2\right)_B^B} = \frac{3}{8i_2^2} \left[(a^2 + 1) - (a^2 - 1)^2 \left(\frac{1}{a} \tanh^{-1} \frac{1}{a}\right) \right]$$

$$\frac{\left(\overline{q_{1}^{2}}\right)_{1}^{C}}{\left(\overline{q_{1}^{2}}\right)_{A}^{A}} = \frac{\left(\overline{q_{1}^{2}}\right)_{1}^{B}}{\left(\overline{q_{1}^{2}}\right)_{A}^{A}} = \frac{v^{2}\eta^{2}}{2\xi^{2}\mu^{2}} \left\{ 3\xi^{2} - 1 + 3(1-\eta^{2}) \left[1 - (\eta^{2}-\xi^{2})\left(\frac{1}{\eta} \tanh^{-1} \frac{1}{\eta}\right)\right] \right\}$$

$$\frac{\left(\overline{q_2}^2\right)_1^C}{\left(\overline{q_2}^2\right)_1^A} = \frac{\left(\overline{q_2}^2\right)_1^B}{\left(\overline{q_2}^2\right)_1^A} = \alpha^2 + \frac{\pmb{v}^2}{8} + \frac{\pmb{v}^2\eta^2}{16\xi^2} \left[\Im(\eta^2 - \xi^2) - 2 \right] - \frac{\Im \pmb{v}^2\eta^2(\eta^2 - 1)(\eta^2 - \xi^2)}{16\xi^2} \left(\frac{1}{\eta} \ \tanh^{-1} \ \frac{1}{\eta}\right)$$

Punched-card equipment was used to obtain the turbulence-velocity ratios listed in table I. For the cases N = 2, 3, and 4, the integrations required for equations (25) and (26) were performed numerically by use of Simpson's rule after changing the variable of integration from θ to x by applying the transformation x = cos θ . Intervals $\Delta x = 0.01$ were used in the range $0 \le x \le 0.9$; intervals $\Delta x = 0.001$ were used in the range $0.9 \le x \le 1.0$. In all computations the Mach number MB upstream of the contraction was taken equal to 0.05. The turbulence velocity ratios listed in table I may be corrected for values of MB other than 0.05 as follows: Values of the parameters l_1^2 , l_2^2 , and $a^2 = \frac{1}{1-\epsilon}$ for MB = 0.05 and for the desired value of MB are obtained from equations (19). Noting that the quantities

$$l_1^2 = \frac{\left(\overline{q_1^2}\right)_N^C}{\left(\overline{q_1^2}\right)_N^A}$$
 and $l_2^2 = \frac{\left(\overline{q_2^2}\right)_N^C}{\left(\overline{q_2^2}\right)_N^A}$ depend only upon a^2 and K, the values

of these quantities for the a^2 corresponding to the desired M_B are obtained from table I. With l_1^2 and l_2^2 known for $M_B = 0.05$ and the desired M_B , the corrected velocity ratios are obtained by simple computation. The following empirical relations (reference 1) were utilized in obtaining numerical results:

$$\alpha^2 = \left(\frac{8-K}{8+K}\right)^2$$
 for $K \le 1$

$$\alpha^2 = \left(\frac{1.21}{1+K}\right)$$
 for $K > 1$

For design purposes, the screen pressure-drop coefficient K may be estimated, according to reference 10, from the solidity ratio b, where b is the area of the holes in a unit area of screen, as

$$K \approx \frac{1 - b}{b^2}$$

For square-mesh screen with wire diameter d and mesh designation m, the solidity ratio as defined is

$$b = (1-md)^2$$

A better agreement with the screen data given in reference 1 is obtained from

$$b \approx (1-md)^{7/4}$$

The variation of the longitudinal and lateral root-mean-square velocity ratio with speed ratio l_1 for a single screen (N=1) upstream of the contraction is plotted in figures 4(a) and 4(b), respectively, for selected values of the screen pressure-drop coefficient K. The results for K = 0, which correspond to the case of stream convergence or divergence in the absence of any screen, are, of course, identical with the results of reference 3. In general, both the longitudinal and the lateral fluctuation velocities downstream of the screen-contraction configuration are reduced as the screen parameter K is increased. The somewhat anomalous trend of the longitudinal velocity ratios for values of the speed ratio less than 2 seems to reflect the variation of the auxiliary screen parameter ξ^2 which approaches zero at K = 2.76, becomes infinitely large in the negative sense as K increases to 5.28, and becomes infinitely large in the positive sense as K decreases to 5.28.

The losses incurred through the use of damping screens are proportional to the product $NKU_A{}^3$, where N denotes the number of identical screens in series (multiple screens) and NK is the over-all screen pressure-drop coefficient. The velocity ratios for a multiple-screen arrangement upstream of a contraction are compared on the basis of equal screen losses in figure 5 for the particular case NK = 6. The advantages of using a number of screens in series to attain a given over-all coefficient NK are obvious. An examination of table I indicates that the use of multiple screens to attenuate the downstream fluctuation velocities becomes more effective as the over-all coefficient NK is increased. The screen losses can be reduced by decreasing the settling-chamber stream velocity U_A . Low-turbulence wind tunnels are generally characterized by their many damping screens and large-cross-sectional-area settling chambers.

One-dimensional spectra. - In accordance with equation (6), the one-dimensional spectra at stations A and B are given by

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$$F_{\gamma}^{A} = 2 \int_{-\infty}^{\infty} \Gamma_{\gamma \gamma}^{A}(\underline{k}) dk_{2}dk_{3}$$
 (29)

and

$$\mathbf{F}_{\mathbf{\gamma}}^{\mathbf{C}} = 2 \int \int_{-\infty}^{\infty} \mathbf{F}_{\mathbf{\gamma}\mathbf{\gamma}}^{\mathbf{C}}(\underline{\mathbf{\kappa}}) \, \mathrm{d}\mathbf{\kappa}_{2} \mathrm{d}\mathbf{\kappa}_{3}$$

As pointed out in reference 3, a comparison of the upstream and down-stream spectra on the basis of the upstream longitudinal wave number k is equivalent to a comparison of the time spectra indicated by fixed hot-wire probes located at the corresponding stations. Defining the downstream spectra $F_{\gamma}^{C}(\mathbf{k}_{1}) \equiv l^{-1}F_{\gamma}^{C}$ such that

 $\int_{0}^{\infty} F_{\gamma}^{C}(k_{1}) dk_{1} = \int_{0}^{\infty} F_{\gamma}^{C}(\kappa_{1}) d\kappa_{1}, \text{ the one-dimensional spectra at station C are given by}$

$$\left[\mathbb{F}_{\Upsilon}^{C}(\mathbf{k}_{1})\right]_{N} = \frac{2}{l_{1}l_{2}^{2}} \int \int \left[\mathbb{F}_{\Upsilon\Upsilon}^{C}\left(\frac{\mathbf{k}_{1}}{l_{1}}, \frac{\mathbf{k}_{2}}{l_{2}}, \frac{\mathbf{k}_{3}}{l_{2}}\right)\right]_{N} d\mathbf{k}_{2} d\mathbf{k}_{3}$$
(30)

Evaluation of equations (29) and (30) requires that the amplitude function G(k) in equation (4) be specified. Compatible with the empirical relation for isotropic turbulence obtained in reference 8, this function is taken to be

$$G(k) = \frac{H}{(k_1^2 + n^2 + \zeta^2)^3}$$
 (31)

where the constants n and H are defined as $n \equiv \frac{1}{(L_1)^A}$ and $H \equiv \frac{2n}{\pi^2} \left(q_1^2\right)^A$.

As shown in appendix C, the one-dimensional spectra obtained from equations (4) and (31) may be expressed in terms of a dimensionless wave number k_1/n as incorporated in the following parameters:

$$s \equiv 1 + k_1^2/n^2$$

$$f \equiv s/\eta^2 + 4/\mu^2$$

$$g \equiv s/\xi^2 + 4\alpha^2/v^2$$

$$h \equiv \frac{1 - a^2 - s^2}{a^2}$$
(32)

Thus the upstream one-dimensional spectra for this special case of isotropic turbulence are, in dimensionless form,

$$\frac{F_1^{A}(k_1/n)}{F_1^{A}(0)} = \frac{1}{s}$$
 (33)

$$\frac{F_2^{A}(k_1/n)}{F_2^{A}(0)} = \frac{3s-2}{s^2}$$
 (34)

Also, the longitudinal one-dimensional spectrum downstream of a single-screen-axisymmetric-contraction configuration may be written (see appendix C) in dimensionless form as

$$\frac{F_1^{C}(k_1/n)}{F_1^{A}(0)} = \frac{2v^2}{l_1^2\mu^2} \left[c_1 + c_2 \log_e \frac{s+h}{s} + c_3 \log_e \frac{4(s-1)}{\mu^2 s} \right]$$
(35)

where

$$\begin{split} & C_1 \equiv \frac{1}{h^3} \left\{ \frac{g(2f-h)}{f^2} + \frac{gh}{2fs} + \frac{h(1+2g)}{f} + \frac{(1+h)^2\mu^2}{v^2} \overline{\left[\frac{a^2(v^2-4\alpha^2)-v^2}{a^2(\mu^2-4)-\mu^2} \right]} \right\} \\ & C_2 \equiv \frac{\mu^2}{h^2 \overline{\left[a^2(\mu^2-4)-\mu^2 \right]}} \left\{ \frac{3sg}{h^2} + \frac{g(s+2)+2s}{h} + 1 - h - \frac{\mu^2(s+h)(g+h)}{h \overline{\left[a^2(\mu^2-4)-\mu^2 \right]}} \right\} \\ & C_3 \equiv \frac{(s-f)(f-g)(\mu^2-4)^2a^4}{f^3 \overline{\left[a^2(\mu^2-4)-\mu^2 \right]^2}} \end{split}$$

The corresponding lateral one-dimensional spectrum is

$$\frac{F_2^{C}(k_1/n)}{F_2^{A}(0)} = \frac{2(s-1)}{l_2^{2}} \left[E_1 + E_2 \log_e \frac{s+h}{s} + E_3 \log_e \frac{4(s-1)}{\mu^2 s} \right]$$
(36)

where

$$\begin{split} E_1 &\equiv \frac{\alpha^2(3s-2)}{2s^2(s-1)} + \frac{(\boldsymbol{v}^2 - \alpha^2 \mu^2)(2s-f)}{2\mu^2 f^2 s} + \frac{2\boldsymbol{v}^2}{a^2 f h} \left[\frac{g(h-f)}{f h} - \frac{g}{2s} - 1 \right] \\ &- \frac{\boldsymbol{v}^2}{2a^4 \mu^2 h} \left[2(s+h) \left\{ \frac{f(g+h) - g(h-f)}{f^2 h^2} + \frac{\mu^2 \left[a^2 (\boldsymbol{v}^2 - 4\alpha^2) - \boldsymbol{v}^2 \right]}{\boldsymbol{v}^2 h^2 \left[a^2 (\mu^2 - 4) - \mu^2 \right]} \right\} + \frac{2h(g-f) - fg}{f^2 h} \right] \\ E_2 &\equiv \frac{(s+h) \left[a^2 (\boldsymbol{v}^2 - 4\alpha^2) - \boldsymbol{v}^2 \right]}{a^2 h^4 \left[a^2 (\mu^2 - 4) - \mu^2 \right]} \left\{ 2h + \frac{3s+h}{a^2} + \frac{4(a^2-1)(\boldsymbol{v}^2 - \alpha^2 \mu^2)h}{\left[a^2 (\mu^2 - 4) - \mu^2 \right] \left[a^2 (\boldsymbol{v}^2 - 4\alpha^2) - \boldsymbol{v}^2 \right]} \right\} \\ E_3 &\equiv \frac{4(s-1)(\boldsymbol{v}^2 - \alpha^2 \mu^2)}{u^4 f^3} \left[1 + \frac{4}{a^2 (\mu^2 - 4) - \mu^2} \right]^2 \end{split}$$

The one-dimensional spectra given by equations (33) to (36) are applicable when the amplitude function G(k) has the particular form of equation (31). Although these spectra are not expected to be valid for the very high wave numbers because of the neglect of viscosity, various experiments on isotropic turbulence have indicated that equations (33) and (34) provide a very good approximation to that portion of the actual isotropic spectrum containing the largest part of the turbulent energy. Equations (35) and (36) should furnish a similar approximation for axisymmetric turbulence. The restrictions given for equations (33) to (36) do not apply to the expressions for turbulence velocity ratios, equations (25) and (26), for which there is no need to particularize the spectrum amplitude function G(k).

The downstream longitudinal and lateral one-dimensional spectra, equations (35) and (36), are compared with the corresponding upstream isotropic spectra, equations (33) and (34), in figures 6(a) and 6(b), respectively, for the following typical case: $\rm M_B=0.05,\,M_C=2.0,\,K=2,\,N=1.$ The case $\rm K=0,$ as obtained in reference 3, has also been included for comparison. The scaling factors indicated by equations (B5) and (B6) of appendix B have been incorporated in the downstream spectral ordinates so that the zero-wave-number intercept gives the turbulence scale ratio (appendix B).

The distortion in shape of the longitudinal spectrum noted in reference 3 as a consequence of the stream convergence is accentuated (fig. 6(a)) by the presence of a damping screen upstream of the contraction. This distortion is accompanied by a reduction in the ordinate values by the factors $\left(\frac{1}{q_1^2}\right)^C / \left(\frac{1}{q_1^2}\right)^A$ and $\left(\frac{1}{q_1^2}\right)^C / \left(\frac{1}{q_1^2}\right)^B$ for K=2 and K=0, respectively. The downstream lateral spectrum ordinates

 $(\frac{\text{fig. }6(b))}{q_2^2})^C/(\frac{1}{q_2^2})^A$ and $(\frac{1}{q_2^2})^C/(\frac{1}{q_2^2})^A$ and $(\frac{1}{q_2^2})^C/(\frac{1}{q_2^2})^A$ for K=2 and K=0, respectively. The distortion in shape is relatively slight compared with the distortion noted for the longitudinal spectrum.

As may be seen from equations (33) and (34) for the upstream isotropic spectra, the longitudinal and lateral spectral ordinates have maximum values at $k_1/n=0$ and $k_1/n=1/\sqrt{3}$, respectively. The situation is reversed for the downstream spectra. Here the lateral spectral ordinates have maximum values at $k_1/n=0$ and the longitudinal spectral ordinates at $k_1/n\approx 1.4$. Occurrence of a peak in the spectrum curve at some wave number other than zero is an indication that the correlation coefficient may take on negative values.1

Scale ratios and correlation coefficients. - For the scales of turbulence defined by equation (10), the longitudinal and lateral turbulence scale ratios (ratios of downstream to corresponding upstream scales) for a screen-contraction configuration are obtained in appendix B as

$$\frac{\left(L_{1}\right)_{N}^{C}}{\left(L_{1}\right)^{A}} = \left(\frac{v^{2}}{\mu^{2}}\right)^{N} \left[l_{1}^{2} \frac{\left(\overline{q_{1}^{2}}\right)_{N}^{C}}{\left(\overline{q_{1}^{2}}\right)^{A}} \right]^{-1}$$
(37)

$$\frac{\left(L_{2}\right)_{N}^{C}}{\left(L_{2}\right)^{A}} = \alpha^{2N} \left[l_{2}^{2} \frac{\left(\overline{q_{2}^{2}}\right)_{N}^{C}}{\left(\overline{q_{2}^{2}}\right)^{A}} \right]^{-1}$$
(38)

The scale ratios obtained from equations (37) and (38) which do not require that the amplitude function G(k) of equation (31) be specified are listed in table I for the case of isotropic turbulence at station A. Typical results are plotted in figure 7.

The lateral scale ratio (see fig. 7(a)) approaches a constant value of approximately 4/3 for values of the speed ratio l_1 greater than 3. Measurements of the lateral correlation curve at a speed ratio near unity which are reported in reference 11 indicate that the lateral scale is substantially unchanged by damping screens. This is in qualitative agreement with the present result which indicates that for l_1 slightly greater than unity the downstream lateral scale will not exceed the

For example, when $F_{\gamma}(k_1) = k_1$ e^{-k₁/n}, the correlation coefficient is obtained by using equation (7) as

 $[\]left[\left(\frac{1}{n} \right)^2 + r_1^2 \right]^{-P/2} \Gamma(P) \cos \left(P \, \tan^{-1} \, nr_1 \right) \text{ where } \Gamma \text{ designates the gamma function. For } P = 1, \, R_{\gamma}(r_1) \text{ is always positive; for } P > 1, \, R_{\gamma}(r_1) \text{ will take on negative values for particular values of } r_1.$

corresponding upstream scale by more than about 20 percent. Taking the lateral scale ratio equal to 4/3 leads to the following convenient approximation for the lateral turbulence velocity ratio from equation (38):

$$\frac{\left(\overline{q_2^2}\right)_N^C}{\left(\overline{q_2^2}\right)^A} \approx \frac{3\alpha^{2N}}{4l_2^2} \tag{39}$$

For a given value of the screen pressure-drop coefficient NK, the longitudinal scale ratio (see fig. 7(b)) decreases with increasing speed ratio l_1 to a minimum value at $l_1=27.4$ (corresponding to $M_B=0.05$, $M_C=\sqrt{3}$) where the contraction parameter a^2 has its minimum value. As shown in table I, the longitudinal scale ratio attains a zero value when the screen parameter $v^2=0$ (K ≈ 2.76). This and the occurrence of maximums in the downstream longitudinal spectrum curves at nonzero wave numbers suggest that the downstream longitudinal correlation coefficients are negative for extensive ranges of the separation distance r_1 . Under these conditions interpretation of the conventionally defined scales as lengths characteristic of the average size of the turbulence eddies is open to question, and consideration of the correlation coefficient curves is advisable.

The correlation coefficients at station A for isotropic turbulence with the spectrum amplitude function G(k) given by equation (31) are obtained from equation (7) as

$$R_{1}^{A} = e^{-r_{1}n} \tag{40}$$

$$R_2^A = \left(1 - \frac{r_1^n}{2}\right) e^{-r_1^n} \tag{41}$$

The contour integrations used to obtain equations (40) and (41) are not valid when r_1 = 0; hence the microscales λ_{γ} are evaluated from the integral relation of equation (9). Such evaluations indicate that $\lambda_1^A = \lambda_2^A = 0$, which is to be expected in view of the neglect of viscosity effects in the analysis. The longitudinal correlation coefficient curve of equation (40) is plotted in figure 8(a) and is always positive; the lateral correlation coefficient curve of equation (41) plotted in figure 8(b) reaches its zero value at $r_1^n = 2$ $(r_1 = 2L_1^A)$ and its minimum value at $r_1^n = 3$ $(r_1 = 3L_1^A)$.

The downstream correlation coefficient curves (at station C) have been obtained numerically for the case N = 1 from the following rearrangement of equations (7):

$$R_{1}^{C}(\mathbf{r}_{1}n) = \frac{2}{\pi} \int_{0}^{\infty} \frac{F_{1}^{C}(\frac{\mathbf{k}_{1}}{n})}{F_{1}^{A}(0)} \frac{\left(\overline{\mathbf{q}_{1}^{2}}\right)_{1}^{C}}{\left(\overline{\mathbf{q}_{1}^{2}}\right)_{A}^{A}} \cos \mathbf{k}_{1}\mathbf{r}_{1} d\left(\frac{\mathbf{k}_{1}}{n}\right)$$
(42)

$$R_{2}^{C}(\mathbf{r}_{1}n) = \frac{1}{\pi} \int_{0}^{\infty} \frac{F_{2}^{C}(\frac{\mathbf{k}_{1}}{n})}{F_{2}^{A}(0)} \frac{\left(\overline{\mathbf{q}_{2}^{2}}\right)_{1}^{C}}{\left(\overline{\mathbf{q}_{2}^{2}}\right)^{A}} \cos \mathbf{k}_{1}\mathbf{r}_{1} d\left(\frac{\mathbf{k}_{1}}{n}\right)$$
(43)

In evaluating equations (42) and (43), values of the integrand were obtained for k_1/n ranging from 0 to 50; and for k_1/n greater than

50, in view of the asymptotic behavior of the functions $\frac{F_{\gamma}(\frac{1}{n})}{F_{\gamma}^{A}(0)} \frac{(q_{\gamma}^{2})_{1}}{(q_{\gamma}^{2})^{A}}$

the integrand was approximated as $\frac{\cos k_1 r_1}{(k_1/n)^2}$. Typical downstream longi-

tudinal and lateral correlation coefficient curves (for the case MB = 0.05, MC = 2.00, K = 2, N = 1) are also plotted in figures 8(a) and 8(b), respectively, to indicate the changes resulting from passage of initially isotropic turbulence through a given screen and contraction. Although the downstream lateral correlation coefficient is shown in figure 8(b) to reach slightly negative values, it is believed that these are the result of unavoidable "round-off" errors in computation of the Fourier transforms and that the coefficient is actually always positive, consistent with the corresponding spectrum curve of figure 6(b), which has its maximum value at zero wave number.

The correlation between simultaneous fluctuation velocities at two points a distance \mathbf{r}_1 apart will decrease more rapidly with increasing values of \mathbf{r}_1 when the eddies comprising the turbulent field are small than when the eddies are large. Figure 8(a) thus indicates that the longitudinal scale of an initially isotropic field of turbulence is decreased by passage through the particular screen-contraction configuration chosen. Figure 8(b) indicates that the corresponding lateral scale is increased.

In view of the negative values attained by the downstream longitudinal correlation coefficient, no physical meaning can be assigned to the longitudinal scale ratio defined in the conventional manner by equation (10). For example, the longitudinal scale ratio reaches a zero value even though the longitudinal turbulence velocity ratios are finite when the screen pressure-drop coefficient NK has the value 2.76. The negative values attained by the upstream lateral correlation coefficient do not present a similar anomaly because of the relation between the longitudinal and lateral scales in the case of isotropic turbulence, namely, $L_1^A = 2L_2^A$.

The difficulty is removed if an effective longitudinal scale L_1 ' is defined as the positive area under the corresponding correlation curve. Effective longitudinal scale ratios are plotted in figure 9 and show a qualitative similarity with the conventional ratios shown in figure 7(b). For a given value of the screen pressure-drop coefficient NK, the effective scale ratio decreases with increasing speed ratio l_1 to a minimum value at $l_1 = 27.4$ for which the contraction parameter a^2 has its minimum value. For a given contraction the effective scale ratio reaches its minimum value when NK ≈ 2.76 .

ESTIMATION OF DECAY EFFECTS

In view of the assumptions of inviscid flow and small fluctuation velocities relative to the main stream, the preceding analysis is strictly applicable only in the absence of the turbulent decay processes (viscous dissipation and turbulent mixing). For many wind-tunnel configurations, effects of decay upon turbulence are of the same order of magnitude as the screen-contraction effects. Correction of the theoretical turbulence velocity ratios may therefore prove necessary for practical applications of the theory.

Selection of the appropriate decay correction presents certain difficulties inasmuch as there is a lack of experimental investigations of axisymmetric turbulence decay. Some guidance may be obtained from the theoretical studies of Batchelor (reference 4) and Chandrasekhar (reference 12) on axisymmetric turbulence. The time rates of change of the mean-square velocity components are, in the notation of reference 4:

$$\frac{d}{dt} \left(\overline{u_1^2} \right) = -4m_0 + 2v(-10a - 2b - 2c - 14d)$$

$$\frac{\mathrm{d}}{\mathrm{dt}} \left(\overline{u_2^2} \right) = 2m_0 + 2v \left(-10a + b - 3d \right)$$

In these equations and in equations (44) and (45), the symbol ν represents the kinematic viscosity coefficient. The corresponding expression for the mean-square resultant velocity is

$$\frac{d}{dt} \left(\overline{u_1^2} + 2\overline{u_2^2} \right) = -2v(30a + 2c + 20d)$$
 (44)

For isotropic turbulence, c = d = 0 and equation (44) becomes

$$\frac{\mathrm{d}}{\mathrm{dt}} \left(\overline{u_1^2} + 2\overline{u_2^2} \right) = \frac{\mathrm{d}}{\mathrm{dt}} \left(3\overline{u_1^2} \right) = -2v(30a) \tag{45}$$

The velocity components $\overline{u_1}^2$ and $\overline{u_2}^2$ of reference 4 are identical with $\overline{q_1}^2$ and $\overline{q_2}^2$ in the present notation. The quantities a, b, c, and d in appropriate groupings represent the coefficients in the series expansions in r_1 for the longitudinal and lateral velocity correlation coefficients. The quantity m_0 depends on the two-point velocity-pressure correlation which tends to zero as isotropy is approached. For the decay of isotropic turbulence in a constant-area channel during the initial period wherein both inertia and viscous forces are of importance, equation (45) leads to the semiempirical relation (reference 13)

$$\frac{1}{3} \left[\frac{\overline{q_1^2}}{(\overline{q_1^2})^A} + 2 \frac{\overline{q_2^2}}{(\overline{q_2^2})^A} \right] = \left\{ 1 + \frac{0.58t(l_1)}{L_2^A} \left[(\overline{q_1^2})^A \right]^{1/2} \right\}^{-1} \equiv J \quad (46)$$

where $\overline{q_1^2}$ and $\overline{q_2^2}$ represent the mean-square velocity components at any station downstream of the reference station A and $t(l_1)$ represents the appropriate decay time.

The absence of the velocity-pressure correlation term $m_{\rm O}$ in both equations (44) and (45) suggests that, provided the quantity (2c + 20d) is much smaller than the quantity 30a, equation (46) may yield a satisfactory approximation for the decay of the mean-square resultant turbulent velocity in axisymmetric turbulence. The data of references 1 and 14 tend to support such an approximation. The assumption that the effects of the screen-contraction combination and the decay upon the turbulent velocity ratios proceed independently (see reference 3) leads to the relation

$$\frac{1}{3} \left[\frac{\left(\overline{q_{1}^{2}}\right)_{N}^{C}}{\left(\overline{q_{1}^{2}}\right)^{A}} + 2 \frac{\left(\overline{q_{2}^{2}}\right)_{N}^{\overline{C}}}{\left(\overline{q_{2}^{2}}\right)^{A}} \right|_{scd} = \frac{J}{3} \left[\frac{\left(\overline{q_{1}^{2}}\right)_{N}^{C}}{\left(\overline{q_{1}^{2}}\right)^{A}} + 2 \frac{\left(\overline{q_{2}^{2}}\right)_{N}^{\overline{C}}}{\left(\overline{q_{2}^{2}}\right)^{A}} \right]_{sc}$$
(47)

where the subscript sc refers to the turbulence velocity ratios obtained in the absence of decay, computed from equations (25) and (26) and listed in table I, and the subscript scd implies that the effects of initial period decay have been included. In computing J from equation (46), the decay time $t(l_1)$ is taken as the time required for a particle at local main-stream velocity to pass through the screens and the contraction starting from station A. This implies that the contraction affects only the decay time. Some question exists as to the applicability of equation (46) and hence equation (47) for damping screens in which the wire diameters are usually very small.

A comparison of the theoretical mean-square resultant turbulence velocity ratio corrected for decay by the use of equation (47) with the experimental ratios obtained from reference 1 is shown in figure 10. The mean-square resultant velocity in the absence of decay for the case of a single-screen-contraction configuration (N=1) is also included to show the magnitude of the correction involved for the configuration of reference 1. The following data were used in applying the decay correction: $U_A = 62.8$ feet per second, $\left[(\overline{q_1^2})^A \right]^{1/2} = 0.15$ foot per second; and $L_2^A = 0.05$ foot (estimated). The screen pressure-drop coefficients were corrected as suggested in reference 14

$$K = K_e + \frac{U_A}{2} \frac{dK_e}{dU_A}$$

where $K_{\rm e}$ designates the screen pressure-drop coefficient measured at a given speed $U_{\rm A}$. Although the single experimental points obtained for each multiscreen arrangement do not check the decay correction as well as do those for the single-screen arrangement, the limited data do not warrant any refinement of the correction method for multiscreen-contraction configurations.

In order to obtain the resolution of the resultant turbulence velocity ratio into longitudinal and lateral components, some knowledge of the velocity-pressure correlation is required. As shown in reference 4 the effect of this correlation as represented by the term \mathbf{m}_{O} is to transfer energy from the larger to the smaller of the velocity components, thus providing a drive towards isotropy. As shown in table I, the longitudinal component will, in general, be much smaller than the lateral component so that adjustment of the longitudinal component is more critical than adjustment of the lateral component. The magnitude of the longitudinal component is governed by two opposing effects. Turbulent decay processes reduce this component; the drive towards isotropy tends to increase it. In the absence of any quantitative knowledge concerning the velocity-pressure term m_{O} , the simplest assumption to be made is that the longitudinal turbulence velocity ratio may be corrected for decay and isotropy drive by taking an average of the values for zero decay and isotropic decay or

$$\left[\frac{\left(\overline{q_1^2}\right)_N^C}{\left(\overline{q_1^2}\right)_N^A}\right]_{scd} = \left(\frac{J+1}{2}\right) \left[\frac{\left(\overline{q_1^2}\right)_N^C}{\left(\overline{q_1^2}\right)_N^A}\right]_{sc}$$
(48)

Consistent values of the lateral turbulence velocity ratio are then obtained from the longitudinal velocity ratio of equation (48) and the resultant velocity ratio of equation (47).

The comparison shown in figure 11 provides some estimate as to the agreement that might be expected between the predicted turbulence-velocity-ratio components (corrected for decay) and the experimental values. The agreement shown is considered satisfactory for most engineering applications. The theoretical velocity ratios obtained in the absence of decay are included for the case N=1 to indicate the magnitude of the correction.

The turbulence scales are also affected by the turbulence decay process, tending to increase as the decay time is increased. Under the action of the viscous forces the smallest eddies are dissipated so that the average eddy size (scale) would be expected to increase. For isotropic turbulence, the change in scale during the initial period analogous to the relation given for the fluctuation velocity, equation (46), is

$$\left(\frac{L_2}{L_2}\right)^2 = J^{-1}$$

Presumably the effect of decay upon the scales of turbulence could thus be obtained by a procedure similar to the one suggested for the fluctuation velocities. In the absence of any experimental data such development does not appear warranted.

CONCLUDING REMARKS

The present analysis treats, in the absence of turbulent decay processes, the combined effect of a series of identical damping screens followed by a stream convergence (or divergence) upon the mean-square fluctuation velocities, scales, correlation coefficients, and one-dimensional spectra of a field of turbulence convected by a main stream. Numerical results are presented for the case of upstream isotropic turbulence.

The limited experimental data available confirm at least qualitatively some of the theoretical results obtained such as the distortion of an initially isotropic field of turbulence by the damping screens and stream convergence into a field axisymmetric about the main-stream direction with the lateral components of the resultant fluctuation velocity larger in magnitude than the longitudinal component, and the relative insensitivity of the lateral scale of turbulence to damping-screen and stream-convergence effects. The beneficial effects of using several screens in series to attain a given over-all screen pressure-drop coefficient in attenuating the fluctuation velocities are also substantiated. This attenuation is accentuated as the screen coefficient NK is increased.

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The theory predicts certain marked changes in the ordinates of the downstream one-dimensional spectra and, in the case of the longitudinal spectra, a noticeable distortion of shape which should be confirmable by experiment. The longitudinal downstream correlation coefficients attain negative values over a large range of the separation distance \mathbf{r}_1 . Under these conditions, the scales of turbulence as conventionally defined cannot be regarded as representative of the average eddy size. Accordingly, the longitudinal scales have been redefined. The effect of the damping screens and stream convergence is to decrease the longitudinal scale and to increase the lateral scale.

An approximate method of correcting the predicted turbulent fluctuation velocities for the effects of turbulent decay is presented. Tabulations of the fluctuation velocities over a wide range of conditions are provided for convenience in engineering applications.

Lewis Flight Propulsion Laboratory
National Advisory Committee for Aeronautics
Cleveland, Ohio, October 28, 1952

APPENDIX A

SYMBOLS

The following symbols are used in this report:

A_{1,2} parameter groupings defined after equation (27)

a² auxiliary contraction parameter, $a^2 \equiv 1/1 - \epsilon$

B_{1,2,3} parameter groupings defined after equation (28)

b solidity ratio of damping screen

C_{1,2,3} parameter groupings defined after equation (35)

D_{1,2,3} edge lengths of volume within which the turbulence field is defined

d wire diameter of damping screen

 $E_{1.2.3}$ parameter groupings defined after equation (36)

 F_{γ} F_1 , F_2 , or F_3

 F_1 one-dimensional longitudinal spectral density (see equation (6))

 $F_{2.3}$ one-dimensional lateral spectral densities (see equation (6))

f auxiliary wave-number parameter, $f \equiv s/\eta^2 + 4/\mu^2$

G(k) amplitude function in isotropic spectrum tensor (see equations (4) and (31))

g auxiliary wave-number parameter, $g \equiv s/\xi^2 + 4\alpha^2/v^2$

H constant appearing in amplitude function of special isotropic spectrum tensor, H $\equiv \frac{2n}{\pi^2} \left(\overline{q_1^2} \right)^A$ (see equation (31))

h auxiliary wave-number parameter, $h \equiv \frac{1 - a^2 - s^2}{a^2}$

i $\sqrt{-1}$

```
J turbulence decay factor (see equation (46))
```

K screen pressure-drop coefficient,
$$K = \frac{\Delta p}{\frac{1}{2} \rho U^2}$$

k amplitude of vector
$$\underline{\mathbf{k}}$$
: $\mathbf{k}^2 = \mathbf{k_1}^2 + \mathbf{k_2}^2 + \mathbf{k_3}^2$

$$\underline{\mathbf{k}}$$
 $\mathbf{k}_{\gamma} = \mathbf{k}_{1}$, \mathbf{k}_{2} , or \mathbf{k}_{3} ; wave-number vector

$$L_{\gamma}$$
 L_1 , L_2 , or L_3

$$L_1$$
 longitudinal scale of turbulence (see equation (10))

$$L_1$$
' effective longitudinal scale of turbulence

$$L_2$$
, L_3 lateral scales of turbulence (see equation (10))

$$l_3$$
 stream height at station C divided by stream height at station B

$${\rm M_{B}}_{,{\rm C}}$$
 stream Mach number at station B, C

m mesh designation of damping screen (reciprocal of center-tocenter distance between neighboring wires)

N number of screens in series (cascade)

n constant appearing in amplitude function of special isotropic spectral tensor, n $\equiv \frac{1}{(L_1)^A}$

P constant

$$\underline{Q}$$
 $Q_{\Upsilon} = Q_1, Q_2, \text{ or } Q_3; \text{ wave-amplitude vector}$

 $q_{\gamma} = q_1, q_2, \text{ or } q_3; \text{ turbulence-velocity-fluctuation vector}$

 $R_{r}(r_{1})$ correlation coefficient (see equation (7))

 $R_{\gamma\delta}(\underline{r})$ correlation tensor, $R_{\gamma\delta}(\underline{r}) \equiv \overline{q_{\gamma}(\underline{x})q_{\delta}(\underline{x}+\underline{r})}$

 $\underline{\mathbf{r}}$ $\mathbf{r}_{\gamma} = \mathbf{r}_{1}, \mathbf{r}_{2}, \text{ or } \mathbf{r}_{3}; \text{ separation vector}$

s wave-number parameter, $s \equiv k_1^2/\gamma^2 + 1$

t time

 $t(l_1)$ decay time

U main-stream velocity

u longitudinal component of combined turbulent velocity fluctuations and potential-flow velocities induced by screen

V₁ longitudinal root-mean-square turbulence velocity ratio (used in table I)

V₂ lateral root-mean-square turbulence velocity ratio (used in table I)

v,w lateral components of combined turbulent velocity fluctuations and potential-flow velocities induced by screen

 \underline{x} $x_{\gamma} = x_1, x_2, \text{ or } x_3; \text{ position vector}$

a screen deflection parameter, $\alpha \equiv \lim_{\psi_1 \to 0} \frac{\tan \psi_2}{\tan \psi_1}$

$$\beta^2$$
 $k_1^2 (k_2^2 + k_3^2)^{-1}$

 $\Gamma_{\gamma\delta}(\underline{k})$ three-dimensional spectral tensor

$$\Delta \qquad \frac{4\alpha^2 \cos^2 \theta + v^2 \sin^2 \theta}{4 \cos^2 \theta + u^2 \sin^2 \theta}$$

 $\delta_{\gamma\delta}$ Kronecker delta; $\delta_{\gamma\delta}=1$ for $\gamma=\delta$ and $\delta_{\gamma\delta}=0$ for $\gamma\neq\delta$

 ϵ axisymmetric contraction parameter, $\epsilon \equiv l_2^2/l_1^2$

 $\xi^2 = k_2^2 + k_3^2$

 η^2 auxiliary screen parameter, $\eta^2 = \frac{\mu^2}{\mu^2 - 4}$

 θ polar angle (see appendix B)

 κ amplitude of vector κ_2 ; $\kappa^2 = \kappa_1^2 + \kappa_2^2 + \kappa_3^2$

 $\kappa_{\gamma} = \kappa_{1}, \kappa_{2}, \text{ or } \kappa_{3}$: wave-number vector at station C

 $\Lambda = \frac{4\alpha^2 k_1^2 + v^2 \zeta^2}{4k_1^2 + \mu^2 \zeta^2} \quad \text{(see equation (22a))}$

 λ_{r} λ_{1} , λ_{2} , or λ_{3}

 λ_1 longitudinal microscale of turbulence (see equation (9))

 $\lambda_{2.3}$ lateral microscales of turbulence (see equation (9))

 μ auxiliary screen parameter, $\mu \equiv 1 + \alpha + K$

v auxiliary screen parameter, $v \equiv 1 + \alpha - \alpha K$

 ξ^2 auxiliary screen parameter, $\xi^2 \equiv \frac{v^2}{v^2 - 4\alpha^2}$

ρ stream density

 $\Sigma = \frac{(v^2 - \alpha^2 \mu^2) k_1^2}{4k_1^2 + \mu^2 \zeta^2}$ (see equation (22b))

main-stream density at station C divided by main-stream density at station B

yolume

φ azimuth angle (see appendix B)

 χ $\chi_{\gamma} = \chi_{1}, \chi_{2}, \text{ or } \chi_{3}; \text{ position vector (see equation (12))}$

 ψ_1 angle to screen normal of flow incidence upstream of screen

 ψ_{2} angle to screen normal of flow emergence downstream of screen

$$\Omega = \frac{k_1^2(1-\epsilon)^2 \zeta^2 - 2k_1^2(1-\epsilon)(\epsilon k_1^2 + \zeta^2)}{(\epsilon k_1^2 + \zeta^2)^2}$$
 (see equation (22d))

 $\underline{\omega}$ $\omega_{\gamma} = \omega_1, \omega_2, \text{ or } \omega_3; \text{ vorticity vector}$

Superscripts:

A station upstream of screens

B station downstream of screens and upstream of contraction

C station downstream of contraction

* complex conjugate

Subscripts:

A station upstream of screens

B station downstream of screens and upstream of contraction

C station downstream of contraction

N number of like screens in series

sc only effects of screens and contraction present

scd effects of screen and contraction corrected for initial period of decay

l longitudinal component

2,3 lateral components

APPENDIX B

TURBULENCE VELOCITY AND SCALE RATIOS

Velocity ratios. - Using spherical polar coordinates

$$k_1 \equiv k \cos \theta$$

 $k_2 = k \sin \theta \cos \varphi$

 $k_3 \equiv k \sin \theta \sin \varphi$

$$k^2 = k_1^2 + k_2^2 + k_3^2$$

equations (23) and (24) may be put in the form

$$\left[\Gamma_{11}^{C}\left(\underline{\mathbf{k}}\right)\right]_{N} = \frac{l_{2}^{2}k^{2}G(k)}{l_{1}} \frac{\Delta^{N}\sin^{2}\theta}{(\epsilon\cos^{2}\theta + \sin^{2}\theta)^{2}}$$
(B1)

$$\left[\Gamma_{22}^{C}(\underline{\kappa}) + \Gamma_{33}^{C}(\underline{\kappa})\right]_{N} = \alpha^{2}\left[\Gamma_{22}^{C}(\underline{\kappa}) + \Gamma_{33}^{C}(\underline{\kappa})\right]_{N-1} + \frac{i_{1}G(k)\left(\nu^{2} - \alpha^{2}\mu^{2}\right)k^{2}\Delta^{N-1}\epsilon^{2}\sin^{2}\theta\cos^{2}\theta}{\left(4\cos^{2}\theta + \mu^{2}\sin^{2}\theta\right)\left(\epsilon\cos^{2}\theta + \sin^{2}\theta\right)^{2}}$$
(B2)

where
$$\Delta \equiv \frac{4\alpha^2 \cos^2 \theta + v^2 \sin^2 \theta}{4 \cos^2 \theta + \mu^2 \sin^2 \theta}$$

The downstream mean-square fluctuation velocities are given by

$$\left(\overline{q_{\gamma^2}}\right)^{C} = \iiint_{-\infty}^{\infty} \Gamma_{\gamma \gamma^{C}}(\underline{\kappa}) d\kappa_{1} d\kappa_{2} d\kappa_{3}$$

analogous to equation (5). Inasmuch as the function G(k) appears in the expressions for the energy spectral densities, the variable of integration will be changed from $\underline{\kappa}$ to k so that

$$\frac{\overline{q_{\gamma}^2}}{{l_1 l_2}^2} = \frac{1}{{l_1 l_2}^2} \iiint_{-\infty} \Gamma_{\gamma \gamma}(\underline{\kappa}) dk_1 dk_2 dk_3. \text{ Noting that}$$

 $dk_1dk_2dk_3 = k^2\sin\theta d\theta d\phi dk$, the downstream mean-square velocity components of the turbulent field are obtained from equations (B1) and (B2) as

$$\left(\overline{q_1^2}\right)_{\mathbb{N}}^{\mathbb{C}} = \frac{1}{l_1^2} \int_0^{\infty} k^4 G(k) \ dk \int_0^{2\pi} d\phi \int_0^{\pi} \frac{\Delta^{\mathbb{N}} \sin^3 \theta \ d\theta}{\left(\epsilon \cos^2 \theta + \sin^2 \theta\right)^2}$$

and, inasmuch as the downstream turbulence will be axisymmetric when the upstream turbulence is isotropic,

$$\left(\overline{q_2 z}\right)_N^C = \left(\overline{q_3 z}\right)_N^C = \alpha^2 \left(\overline{q_2 z}\right)_{N-1}^C + \frac{\varepsilon^2 (\nu^2 - \alpha^2 \mu^2)}{2 z_2^2} \int_0^\infty k^4 G(k) \ dk \int_0^{2\pi} d\phi \int_0^\pi \frac{\Delta^{N-1} \sin^3 \theta \cos^2 \theta \ d\theta}{(4 \cos^2 \theta + \mu^2 \sin^2 \theta)(\varepsilon \cos^2 \theta + \sin^2 \theta)^2}$$

The mean-square velocity components of the upstream isotropic turbulence are obtained by using equation (4) as

$$\left(\overline{q_1^2}\right)^A = \left(\overline{q_2^2}\right)^A = \left(\overline{q_3^2}\right)^A = \int_0^\infty k^4 G(k) \ dk \ \int_0^{2\pi} d\phi \ \int_0^\pi \sin^3\!\theta \ d\theta = \frac{8\pi}{3} \ \int_0^\infty k^4 G(k) \ dk$$

The turbulence velocity ratio or ratio of mean-square fluctuation velocities downstream of a series of N identical screens followed by an axisymmetric contraction to the corresponding upstream fluctuation velocities is then given for the longitudinal and lateral components, respectively, by

$$\frac{\left(\frac{1}{q_1^2}\right)_N^C}{\left(\frac{1}{q_1^2}\right)^A} = \frac{3a^4}{4l_1^2} \int_0^{\pi} \frac{\Delta^N \sin^3 \theta \, d\theta}{(a^2 - \cos^2 \theta)^2}$$
(B3)

$$\frac{\left(\frac{q_{2}^{2}}{Q_{1}^{2}}\right)_{N}^{C}}{\left(\frac{q_{2}^{2}}{Q_{2}^{2}}\right)_{N}^{A}} = \frac{\left(\frac{q_{2}^{2}}{Q_{2}^{2}}\right)_{N-1}^{C}}{\left(\frac{q_{2}^{2}}{Q_{2}^{2}}\right)_{N-1}^{A}} + \frac{3(a^{2}-1)^{2}(v^{2}-\alpha^{2}\mu^{2})}{81_{2}^{2}} \int_{0}^{\pi} \frac{\Delta^{N-1}\sin^{3}\theta\cos^{2}\theta\,d\theta}{\left(4\cos^{2}\theta+\mu^{2}\sin^{2}\theta\right)\left(a^{2}-\cos^{2}\theta\right)^{2}} \tag{B4}$$

where $a^2 \equiv \frac{1}{1-\epsilon}$. The new contraction parameter a^2 is introduced for convenience in subsequent calculations. It may be noted that the velocity ratios are independent of the amplitude function G(k) which appears in both the isotropic and axisymmetric spectral tensors. Equations (B3) and (B4) appear in the text as equations (25) and (26), respectively.

Turbulence scale ratios. - The turbulence scales may be obtained from the energy spectral densities as indicated by equations (6) and (10). Compatible with the formulation

$$\left(\overline{q_{\gamma}^{2}}\right)^{C} = \frac{1}{l_{1}l_{2}^{2}} \int \int \int \mathbf{r}_{\gamma\gamma}^{\mathbf{c}} (\underline{\mathbf{k}}) dk_{1} dk_{2} dk_{3}$$

the longitudinal scale at station C is

$$\left(\mathbf{L}_{1}\right)_{N}^{C} = \frac{\pi}{l_{1}l_{2}^{2}\left(\overline{\mathbf{q}_{1}^{2}}\right)_{N}^{C}} \int_{-\infty}^{\infty} \left\{ \left[\mathbf{r}_{11}^{C}(\underline{\kappa})\right]_{N} \right\}_{\kappa_{1}=0} dk_{2}dk_{3}$$

or, applying equation (24),

$$\left(\mathbf{L}_{1}\right)_{N}^{C} = \frac{\pi}{l_{1}^{2} \left(\overline{\mathbf{q}_{1}^{2}}\right)_{N}^{C}} \left(\frac{\boldsymbol{v}^{2}}{\mu^{2}}\right) \int_{-\infty}^{\infty} \left[\Gamma_{11}^{A}(\underline{\mathbf{k}})\right]_{\mathbf{k}_{1}=0} d\mathbf{k}_{2} d\mathbf{k}_{3}$$

The longitudinal scale at station A is

$$(L_1)^A = \frac{\pi}{\left(\underline{q_1}^2\right)^A} \int_{-\infty}^{\infty} \left[\underline{r}_{11}^A(\underline{k})\right]_{k_1=0} dk_2 dk_3$$

The ratio of longitudinal scale downstream of a series of N identical screens followed by an axisymmetric contraction to the corresponding upstream scale or longitudinal scale ratio is thus

$$\frac{\left(L_{1}\right)_{N}^{C}}{\left(L_{1}\right)^{A}} \equiv \frac{\left[F_{1}(0)\right]_{N}^{C}}{\left[F_{1}(0)\right]^{A}} = \left(\frac{v^{2}}{\mu^{2}}\right)^{N} \left[\imath_{1}^{2} \left(\frac{q_{1}^{2}}{q_{1}^{2}}\right)^{A}\right]^{-1} \tag{B5}$$

The corresponding ratio for the lateral scales is obtained in a similar manner as

$$\frac{\left(\text{L}_{2}\right)_{N}^{C}}{\left(\text{L}_{2}\right)^{A}} \equiv \frac{\left[\text{F}_{2}\left(0\right)\right]_{N}^{C}}{\left[\text{F}_{2}\left(0\right)\right]^{A} \frac{\left(\overline{q_{2}^{2}}\right)_{N}^{C}}{\left(\overline{q_{2}^{2}}\right)^{A}}} = \left(\alpha^{2}\right)^{N} \left[\imath_{2}^{2} \frac{\left(\overline{q_{2}^{2}}\right)_{N}^{C}}{\left(\overline{q_{2}^{2}}\right)^{A}}\right]^{-1} \tag{B6}$$

These relations for the scale ratios do not require that the upstream turbulence be isotropic. Equations (B5) and (B6) appear in the text as equations (37) and (38), respectively.

APPENDIX C

ONE-DIMENSIONAL SPECTRA

With the use of equations (4) and (31), equations (29) can be written

$$F_1^A = 4\pi H \int_0^\infty \frac{\zeta^3 d\zeta}{(k_1^2 + n^2 + \zeta^2)^3}$$

$$F_2^A = F_3^A = 2\pi H \int_0^\infty \frac{(2k_1^2 + \zeta^2)\zeta d\zeta}{(k_1^2 + n^2 + \zeta^2)^3}$$

Integration yields, after use of equation (32),

$$F_{\perp}^{A} = \frac{\pi H}{n^{2} \dot{s}} \tag{C1}$$

$$F_2^A = F_3^A = \frac{\pi H(3s-2)}{2n^2s^2}$$
 (C2)

Equations (33) and (34) follow upon dividing equations (C1) and (C2) by $(F_1^A)_{k_1/n=0}$ and $(F_2^A)_{k_1/n=0}$, respectively.

With use of equations (4) and (B1) and (B2) of appendix B, equations (30) can be written

For the case of a single-screen-axisymmetric-contraction configuration, integration of equations (C3) and (C4) yields equations (35) and (36) of the text, respectively. For the case N = 1, the quantity $({\rm F_2}^{\rm C})_{\rm N-1}$ designates the one-dimensional lateral spectrum downstream of an axisymmetric contraction in the absence of damping screens and may be obtained from reference 3.

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					$v_1^2 \equiv \frac{\left(\overline{q_1^2}\right)}{\left(\overline{q_1^2}\right)}$	$\frac{x}{A}, v_2^2 = \frac{\left(\overline{q_2^2}\right)}{\left(\overline{q_2^2}\right)}$	$\frac{N}{A}$, $M_B = 0.05$			N	ACA
N	к	NK	M _C	11	v ₁ ²	v ₂ ²	$\frac{1}{3}(v_1^2 + 2v_2^2)$	v ₁	V ₂	(L ₁) C (L ₁) A	$\frac{\left(L_{2}\right)_{N}^{C}}{\left(L_{2}\right)_{N}^{A}}$
111111111111111111111111111111111111111	.20 .40 .60 1.00 1.50 2.50 2.76 3.00 4.50 4.50 10,00	0.0 0 .2 0 .4 0 .6 0 1.5 0 2.5 0 2.7 6 3.5 0 4.0 0 4.5 0 1.5 0	0.0 2 3 .0 2 3	0,4 6 4 4 6 4 6 6 4 6 7 6 8 7 7 8 7 8 9 7 8	1.675 369	0.9597 .764930 .618013 .506007 .243305 .184258 .136573 .127578 .112765 .0942868 .078858 .058684	1.198100 .8900645 .670645 .513296 .1912387 .1033077 .09874619 .077348 .077348 .0764811 .064811 .0564320	1.2 9 4 0 1.0 6 7 9 8 8 0 9 7 2 6 5 4 9 0 7 1 7 0 8 1.0 0 6 1.1 7 0 8 1.1 2 6 6 1.1 9 1 6 1.2 6 6 1.2 6 6	0.9796 .87461 .78133 .59323 .4933 .4933 .38637 .37578 .31971 .2808 .2422	2.772000 2.7269870 2.680970 2.682390 2.497543 2.218931 1.603421 .382081 .3156866 1.5147163 2.473735 2.439350 2.67472 2.7549200	0.4836 .54491 .67492 .79834 1.017351 1.090691 1.1098375 1.01736 1.01736
111111111111111111111111111111111111111	0.00 .20 .40 .60 1.00 1.50 2.00 2.50 2.76 3.50 4.00 4.50 6.00	0.00 .20 .60 1.50 2.00 2.76 3.00 3.50 4.00 4.50 1.50	0.0 2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	55,55,55,55,55,55,55,55,55,55,55,55,55,	1.094291 .747277 .509285 .2347649 .0361721 .0014126 .0010895 .0116557 .0254057	761268 .6217258 .514258 .3638496 .195699 .1596490 .146378 .120417 .1088600 .082818	87236293 .5626203 .5126620 .1199220 .1199220 .1100389 .093910 .0779919 .0779919 .0570794	1.0444 .86435 .718445 .170647 .108445 .1445 .1445 .148826	878735292979488 77105292979488 78135292979488 78135292979488	2.44 7 8 5 8 2.39 8 7 1 3 2.34 4 1 4 4 2.20 8 1 3 7 3 1 1.32 5 6 5 3 .29 4 5 9 4 .24 1 9 8 4 1.28 0 2 1 3 1.67 5 5 3 7 2.14 4 2 0 2.35 9 0 7 3 7	.55599 .71999 .834056 1.08991 1.1165 1.1989 1.0434
111111111111111111111111111111111111111	0.00 .20 .40 .60 1.50 2.00 2.76 3.00 4.50 4.50 1.00	0.0 0 .2 0 .6 0 1.0 0 1.5 0 2.0 0 2.7 6 3.0 0 4.5 0 4.5 0 1.0 0	0.000000000000000000000000000000000000	0.6 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1.435 .9880466 .468559 .281698 .033413 .011499 .0110501 .016257 .020777 .032422 .044525	0.9216 .76399379.354163299.38997442.3870844.172.0404.1126.3321.1126.3321.095.88	1.092700 .838479 .653447 .51727 .51727 .221900 1.62299 1.29652 1.18497 .098384 .090274 .090274 .084473 .073644	1.1 9 8 0 .9 9 4 0 .8 2 4 9 .6 8 4 5 .4 7 0 8 .2 9 3 6 .1 2 1 6 .1 0 7 2 .1 0 2 8 .1 1 0 7 2 .1 4 4 1 .2 8 0 1 .2 9 1 2 7 5 .1 4 4 1 .2 1 1 0	0.9600 873060 88338625 .4344061 .440668 .35410 .30410	1.935000 1.883875 1.829321 1.769368 1.623836 1.341826 1.56593 0.00032 1.26938 1.282402 1.544813	.6515 .71675 .71675 .89102 .90673 1.06673 1.12865 1.1408 1.1408 1.1348
111111111111111111111111111111111111111	0.00 .20 .40 .60 1.00 2.50 2.50 2.76 3.00 4.00 4.50 4.50 1.50	0.00 .20 .40 .60 1.00 2.50 2.76 3.00 4.50 4.50 1.00	0.000.0	0000 0770000 770000 770000 770000 770000 770000	1299 771 627119 436591 212269 087003 036888 018279 0114585 013195 013789 016789 020406 030137 040476	0.9209 1 7 .7866404 .5737248 .333191 .2568640 .1968751 .1868751 .161985 .1452480 .105990 .071912	1.046900 .8203009 .5280138 .5280128 .5280128 .44462 .1483520 .1360899 .112610 .1025122 .0807061433	11400 9496 7919 6608 4607 29521 13528 1147 1177 11429 1736 2012	255922 0.9581644 0.958158868 0.9581558868 0.958164 0.95816 0.9	1.279000 1.5710000 1.5110000 1.5110000 1.5110000 1.5110000 1.5110000 1.5110000 1.5110000 1.5110000 1.5110000 1.5110000 1.51100000 1.51100000 1.51100000 1.51100000 1.51100000 1.51100000 1.51100000 1.51100000 1.511000000 1.5110000000 1.5110000000000	1.0 0.25 .75599 .8120 .85599 .9034 .0483 1.0994 11.1327 11.1424 11.1524 11.1620 11.1646 11.1641 11.1640
11 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0.00 .40 .60 1.00 2.50 2.76 3.00 4.50 4.50 10.00	0.0 0 0.4 0 0.6 0 1.0 0 2.5 0 2.5 0 2.7 6 3.0 0 4.5 0 4.5 0 1.0 0	0.0 4 0 .0 4 0	.800 .800 .800 .800 .800 .800 .800 .800	1184 829528 826550 410177 204891 008214 040297 021625 0175545 015745 015448 020284 0202847	0.936651 0.698934 0.698934 0.699305 0.469528 0.356206 0.2866179 0.221080 0.206579 0.182188 0.163437 0.148568 0.117924 0.078441	1.019100 .814073 .660173 .542929 .881316 .266894 .153239 .142968 .114780 .105807 .088058	1.09	19978 19978 19978 19979 19	1.3 2 0 0 0 0 0 1 2 6 2 1 9 4 1.2 0 1 7 4 3 1.1 3 6 8 3 3 2 2 7 3 7 6 7 5 2 2 6 2 6 2 7 1 6 7 1 6 7 1 6 8 9 7 1 6 5 1 6 3 1 6 7 1 6 8 9 7 1 6 5 1 6 7	0.8547 .8947 .9370 .9721 1.0370 1.1545 1.1745 1.1846 1.1846 1.1847
111111111111111111111111111111111111111	0.00 .40 .60 1.50 2.50 2.50 2.76 3.50 4.50 4.50 1.50	0.0 0 0.3 0 0.4 0 0.6 0 1.5 0 2.0 0 2.5 0 2.7 6 3.0 0 4.5 0 4.5 0 1.5 0	040 0.045 .045 .045 .045 .045 .045 .045	0.9 0 0 .9 0 0 .0 0 0 0 .0 0 0 .0 0 0 .0 0 0 .0 0 0 .0 0 0 .0 0 0 0 .0 0 0 0 .0 0 0 0	1.086 .767481 .544412 .387481 .198657 .089450 .043450 .024720 .020324 .016989 .018197 .020307 .026853	0.9642 0.8402135 0.640297 0.6406297 0.78689046 0.644985 0.2644985 0.262221 0.1814592 0.162998 0.063890 0.	1.0 1.5 2.0 1.4 1.5 1.5 2.0 1.4 1.5 1.5 2.5 1.4 1.5 1.5 1.5 1.5 1.5 1.5 1.5 1.5 1.5 1.5	1.04261 .04261 .04261 .04261 .04261 .04499 .0449	960857379667761 98150123144895502 98150123144895502 99.887.6555.4.4.4.692	1.291971 1.1377000 1.1377014 1.016092199 .80544077 .2866337 .04028819 .05034819 .05034819 .05034819 .05034819 .05034819 .05034819 .05034819	1.1 2 19 0.9 3 3 7 1.0 0 0 8 1.0 2 8 9 1.0 7 5 3 1.1 1 5 2 2 1.1 7 4 4 1.1 8 2 7 1.1 8 8 8 1.1 9 7 3 1.2 0 3 0 1.1 9 6 7
111111111111111111111111111111111111111	0.00 .40 .600 1.000 1.500 2.000 2.500 2.76 3.000 4.500 6.000	0.00 0.20 0.40 0.60 1.00 1.50 2.00 2.76 3.00 3.50 4.50 6.00 1.00	0.0555555555555555555555555555555555555	01.100 1.100 1.100 1.100 1.100 1.100 1.100 1.100 1.100 1.100 1.100 1.100 1.100	0.9 24 9 6 .6 65 11 8 .4 8 1 9 9 6 .3 4 9 7 2 3 6 .0 9 1 2 0 4 .0 2 9 9 3 3 .0 2 9 6 2 3 .0 2 9 6 2 8 .0 2 9 6 2 8 .0 2 9 6 2 8 .0 2 9 6 2 2	1.0 428 .9 23890 .9 23892 .7 305183 .4 54 2151 .3 714 5766 .2 73075 .2 416489 .1 964489 .1 964480 .0 99685	1.00 3 5 0 0 0 3 5 0 0 0 3 5 0 0 0 3 5 0 0 0 7 6 9 2 2 7 4 4 6 5 0 7 8 2 1 9 2 4 6 9 6 2 1 1 5 7 8 1 1 4 4 1 0 7 6 1 1 3 1 1 4 1 0 7 6 1 1 3 1	1.851 0.96155 6.9410 3.5943 3.2205 1.7582 1.4925 1.1400 1.1458 1.721	1.0 619 .9 6169 .8 5427 .7 6240 .6 6400 .5 4223 .5 4223 .4 6532 .4 4529 .3 15	110 69 59 0.89 37 70 0.89 37 70 0.89 32 720 0.76 64 556 0.57 07 586 1.71 3223 0.0004 0.01 79 43 1.46 49 04 85 61 71	1.1967 1.1606 1.0573 1.0574 1.0574 1.0574 1.10574 1.1143 1.1718 1.1728 1.12073 1.2185 1.2185 1.2295 1.2313 1.2313

TABLE I. - Continued. TURBULENCE VELOCITY AND SCALE RATIOS

					$ v_1^2 = \frac{\left(\overline{q_1^2}\right)_N^C}{\left(\overline{q_1^2}\right)^A} $, $v_2^2 \equiv \frac{\left(\overline{q_2^2}\right)_N^C}{\left(\overline{q_2^2}\right)^A}$, M _B = 0.05			NA	SA-
N	к	NK.	M _C	11	v ₁ ²		$\frac{1}{3}(v_1^2 + 2v_2^2)$	v ₁	v ₂	$\frac{\left(L_1\right)_{N}^{C}}{\left(L_1\right)^{A}}$	$\frac{\left(L_{2}\right)_{N}^{C}}{\left(L_{2}\right)^{A}}$
111111111111111111111111111111111111111	0.00 .20 .40 .60 1.50 2.00 2.76 3.00 4.50 4.50 10.00	00.00 0.20 0.40 0.60 1.50 2.50 2.76 3.00 4.50 4.50 1.00	0.060 .060 .060 .060 .060 .060 .060 .06	01.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 01.400	0.8 52 0 2 7	1.0 7 6 7 8 8 8 7 7 7 4 0 8 8 7 7 7 4 0 8 9 3 6 1 5 7 7 6 2 8 9 3 6 1 5 7 1 9 8 6 7 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 7	1015264 509095 509095 509095 509095 509095 6020745599224 509095	0.9.7.7.3.6.9.9.1.1.6.5.4.2.8.9.9.1.1.6.5.4.2.8.9.1.1.6.5.4.2.8.9.1.1.6.5.4.2.8.9.1.1.5.6.6.3.9.6.6.3.9.6.6.9.9.9.9.9.9.9.9.9.9	1.0 4 4 6 9.9 8 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0.80 95 00 74 813 28 68 6330 21 315 94 08 0.18 00 03 0.14 00 015 1.15 77 66 3.26 20 77 74 76 88 37 0.68	1.0 9 9 0 1.1 1 6 9 1.1 1 6 9 7 1.1 1 4 6 6 7 1.1 1 9 2 2 1.2 2 9 1 7 1.2 2 6 6 5 1.2 4 4 2 8 1.2 4 4 4 0 1.2 4 4 4 0 1.2 4 5 6 6
111111111111111111111111111111111111111	0.00 20 40 40 1.00 1.50 2.50 2.76 3.00 4.50	0.00 0 0.4 0 0.6 0 1.5 0 2.5 0 2.7 6 3.0 0 4.5 0 4.0 0 4.5 0 10.0 0	0.0 70 0 0.0 70 0	1.400 1.400 1.400 1.400 1.400 1.400 1.400 1.400 1.400 1.400	54062852828 430434454 43028525056 43028525056 005559514 005559595 0028210 0028210 002825 002825 002825 002825	1.074490 9490 94447 945884457 946588458 956689 956689 95748 95748 95749	10978267 17782667 18978267 18978267 18978267 18978267 1897826 1897826 1897826 1897826 1897826 1897826 1897826 18986 18986 18986 18986 18986 18986 18986 18986 18986 18986	0.7 0.7 0.7 0.7 0.7 0.7 0.7 0.7 0.7 0.7	10000000000000000000000000000000000000	3559965185596 3559965185596 35599651859596 355999599599599 359999599999 3599999999	11.19.7 6.65.0 1.7 1.11.2 1.2 1.2 1.2 1.2 1.2 1.2 1.2 1.2
111111111111111111111111111111111111111	0.00 20 40 60 1.00 1.50 2.50 2.76 3.50 4.00 4.50 6.00 1.000	0.0 0 2.0 0 1.0 0 1.5 0 2.5 0 2.7 6 3.0 0 3.5 0 4.5 0 6.0 0 1.0 0	0.1 0 0 1.0 0	0.000 2.	0.51 5.90 0.39 2.89 4 0.28 3.4 9.6 0.28 3.4 3.8 8.6 0.08 4.5 3.6 0.05 4.7 0.5 0.03 0.7 0.5 0.03 0.7 0.7 0.7 0.02 0.7 3.7 5 0.02 0.7 9.8 2 0.01 8.9 7.8 0.01 0.03 1.6 1.8 0.03	1.576 77783 1.42843464 1.4284341404 1.428441404 1.53448466 1.5348484 1.454677 1.464477 1.464473 1.4644	1.07567386 .9507386 .677386 .67700144668 .342147406 .342147406 .285523316 .285523316 .181812	0.548437903672256448793365447733867111133887	11.07.769.3259.58 2.93.769.3259.58 2.93.77.084.015.29 2.93.77.084.015.75 2.93.77.084.11.10.75 2.93.77.70.84.11.10.75 2.93.84.11.10.75 2.93.84.11.10.75 2.93.84.11.10.75	427448 372391 320235 2225516 1223241 0005000 000000 034799 1393737 424973 3369800	1.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2
11 11 11 11 11 11 11 11 11 11 11 11 11	.20 .40 .60 1.00 1.50 2.50 2.76 3.50 4.00 6.00	20 .400 1.00 1.500 2.500 2.76 3.000 4.500 4.500	.140 .140 .140 .140 .140 .140 .140 .140	2.77.99.99.99.99.99.99.99.99.99.99.99.99.	0.271092 0.214389 0.171163 0.172956 0.070956 0.048897 0.031984 0.0288359 0.0241337 0.015954 0.015954 0.013246	1.920472 1.7369980 1.569980 1.2816813 .853075 .739952 .6799952 .638976896 .5676896 .364349 .231654	1.37 0 6 7 9 0 1.22 9 1	32629794416431464197326297314641597326297314557	1.3617301 1.25301 1.012360 0.852460 0.75346 0.75346 0.761136 0.600313 1.6571	3167563 26237172 3223717713 307751376 30000144 30184478 30777471 32969432 3310900	1,3 0 5 8 1,3 0 6 7 0 1,3 0 8 9 3 1,3 1 0 0 4 1,3 1 1 1 7 1,3 1 1 2 7 1,3 1 1 3 7 1,3 1 4 9 1,3 1 6 9 1,3 1 6 9
1	0.00 .200 .200 .600 1.500 2.500 2.500 2.76 3.500 4.500 4.500 4.500	0.0 0 .2 0 .6 0 1.0 0 2.5 0 2.5 0 2.7 6 3.0 0 4.5 0 4.5 0	0.180 1.800 1.800 1.800 1.800 1.800 1.800 1.800 1.800 1.800 1.800	03.589 3.589 3.589 3.589 3.589 3.589 3.589 3.589 3.589 3.589 3.589 3.589	0.199161 0.1604483 0.01304483 0.0586491 0.0586447316 0.0218278 0.0215599 0.0168890 0.0168890 0.013556	2.4 24 26 96 3 2.1 98 34 96 8 2.1 98 34 96 8 1.9 83 91 95 1 36 68 3 1.0 27 95 1 36 68 3 1.0 27 95 1 36 68 3 86 19 32 20 47 1 2.5 86 23 8 4.2 93 44 1	1.682657 1.56826724 1.51658643 1.883649 .6273649 .6273649 .548665 .54866596 .4377814 .312349	44061767 36404184 227682 21660703 116477304 113366 1110	1.4810 1.4802 1.40284 1.273898 1.103598 99884 99898 884047 76797 .542	2611667 211675472 117755473 .01557353453 .00000462 .01259266 .05531445	1.3196 1.31200 1.32004 1.32211 1.32211 1.32217 1.32222 1.32222 1.32222
	0.00 1 .20 1 .40 1 .60 1 1.50 1 2.00 1 2.50 1 2.76 1 3.60 1 3.50	00.00 .20 .40 .40 1.00 2.00 2.50 2.50 3.00 4.50 4.50 6.00	0,300 0,00 0,00 0,00 0,00 0,00 0,00 0,00 0,00 0,00 0,00 0,00 0,00	0 5.9 4 8 5.9 4 8	0.12130 .099410 .082410 .068214 .0343792 .02037789 .0183625 .01425224 .0112527 .008704	4.2 8 3 3.8 7 4 7 1 4 3.5 0 5 4 2 9 3.1 7 0 5 4 4 8 2.5 7 0 4 4 8 2.0 7 2 4 8 0 1.7 2 7 4 8 0 1.4 8 0 2 6 5 1.3 7 7 8 8 9 1.1 5 1 2 6 4 1.0 3 6 1 9 0 4 7 4 0 0 7 9	2.89 5 8 0 0 2.61 6 2 9 9 2.3 6 4 4 2 2 3 2.1 6 3 4 4 2 1 7 4 2 1 7 1 1 1 5 9 3 1 7 1 1 1 5 9 3 1 7 1 4 6 7 6 2 2 9 3 1 6 9 1	0.3 4 8 5 4 1 4 4 8 4 8 5 7 8 8 6 2 8 6 2 8 6 5 7 8 1 1 1 0 9 7 7 1 1 1 0 9 7 7 1 1 1 0 9 7 7 1 1 1 0 9 7 7 1 1 1 0 9 7 7 1 1 1 0 9 7 7 1 1 1 0 9 7 7 1 1 1 0 9 7 7 1 1 1 0 9 7 7 1 1 1 0 9 7 7 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 0 9 7 7 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	2.9 7 6 8 4 3 1.0 7 6 8 9 5 6 1.6 0 9 5 6 1.4 3 1 4 7 8 8 1 1.1 3 8 1 1.1 3 7 8 1 1.1 3 7 9 9 7 0 0 2 6 8 6 8 6 8 6 8 6 8 6 8 6 8 6 8 6 8 6	0.2 9 0 7 9 0 6 9 9 9 0 7 9 0 6 9 9 7 9 0 6 9 9 7 9 0 6 9 9 9 1 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	1.3290 1.33001 1.33002 1.33002 1.33002 1.33002 1.33003 1.333004 1.333004 1.333004 1.333004
	1 4.50 4.50 1 6.00 1 0.00 1 .40 1 .40 1 1.50 1 1.50 1 2.50 1 2.76 1 3.50 1 3.50 1 4.50 1 4.50 1 1.00 1 1.00	1.00 0 2.00 0 4.00 1.00 0 1.00 0 2.00 0 2.50 0 3.50 0 4.50 0 4.50 0 1.00 0	0.340 0.340 0.340 0.340 0.340 0.340 0.340 0.340 0.340 0.340	5.9 4 8 0.67 2 4 6.7 2 4	0.10125 .0830241 .0630141 .058073 .041873 .0295531 .017778 .016052 .014737 .0126052 .019880 .007657 .005190	4.770 4.3 2 2 6 2 9 3.9 1 0 6 7 8 3.5 3 7 9 9 2 2 2.3 1 2 2 1 3 8 1.9 2 5 1 3 8 1.9 2 5 1 4 7 9 1.5 3 7 5 2 2 5 1.2 8 4 4 4 5 9 1.1 5 5 0 8 8 2 8 2 5 3 9 4	3213802 22039166 23737422 1.551276 1.291912 1.03912 1.	0.318829 .246416 .246419 .171944 .12112514 .1105945 .0770	2.1 8 4 0 2.0 7 9 7 5 1.8 8 0 0 0 1.5 2 0 8 6 1.3 8 8 1 1.2 3 9 9 1.2 0 3 2 3 1.0 7 5 2 1.0 2 6 8 7 2 4	0.218300 1784497 1143355 1158448 0.019937 0.0100725 0.000725 0.010508621 0.051743	1,3310 1,3311 1,3311 1,3311 1,3311 1,3311 1,3311 1,3312 1,3312 1,3312 1,3312 1,3312 1,3312 1,3312 1,3312

TABLE I. - Continued. TURBULENCE VELOCITY AND SCALE RATIOS

				IMBLE 1.	- continued.	TURBULENCE VE	Process was been	TIE WALLOS			
					$v_1^2 = \frac{\left(\overline{q_1^2}\right)_N^2}{\left(\overline{q_1^2}\right)^A}$	$\left(\frac{1}{q_2}\right)^{\alpha}$; I, M _B = 0.05			NA.	CA.
N	к	NK	M _C	11	v ₁ ²	v ₂ ²	$\frac{1}{3}(v_1^2 + 2v_2^2)$	v ₁	v ₂	$\frac{\left(L_1\right)_{N}^{C}}{\left(L_1\right)_{N}^{A}}$	$\frac{\left(L_{2}\right)_{N}^{C}}{\left(L_{2}\right)^{A}}$
111111111111111111111111111111111111111	9.00 .20 .40 .60 1.00 2.50 2.76 3.50 4.00 4.50 1.00	0.0 0 .2 0 .4 0 .6 0 1.0 0 2.5 0 2.7 6 3.0 0 3.5 0 4.0 0 4.5 0 10.0 0	0.500 .500 .500 .500 .500 .500 .500 .50	09.7 61 9.7 61	0.05604 .046780 .039456 .033540 .024714 .017857 .013756 .011116 .010099 .009314 .008025 .007066 .006330 .004892 .003225 .0032340	6.4 92 5.8 74 4 5 7 5.3 14 6 5 0 4.8 0 6 9 7 9 3.9 2 7 4 9 6 2.6 18 5 8 5 2.2 44 4 9 6 2.0 8 9 2 8 9 1.9 6 3 9 3 1 1.7 4 5 7 1 1 1.5 7 1 1 3 0 3 1.1 2 2 3 2 3 7 1 4 7 9 7	4.346700 3.931898 3.556252 3.215833 2.626569 2.100826 1.7503036 1.396226 1.312391 1.166482 1.049780 .954312 .7497866	0.2367 .2163 .1986 .1831 .1572 .1336 .1173 .1054 .0965 .0841 .0796 .06599	2.5 4 8 0 2.4 2 3 7 2.3 0 5 4 2.1 9 2 5 1.9 8 1 8 1.7 7 2 7 1.4 9 8 2 1.4 4 5 4 1.4 0 1 4 1.3 2 5 3 4 1.1 0 5 9 4 1.0 5 9 4	0.187400 .150331 .119194 .093389 .055034 .024476 .007688 .000787 .000000 .004561 .011148 .019158 .045397	1,3320 1,3325 1,3325 1,3325 1,3325 1,3325 1,3325 1,3325 1,3325 1,3325 1,3325 1,3326 1,3326 1,3326
11111111	0.00 .40 .40 1.00 1.50 2.50 2.76 3.00 4.50 4.50	0.0 0 ,2 0 ,6 0 1.0 0 2.5 0 2.7 6 3.0 0 3.5 0 4.5 0 6.0 0	700 700 700 700 700 700 700 700 700 700	9,761 13,363 13,363 13,363 13,363 13,363 13,363 13,363 13,363 13,363 13,363 13,363 13,363 13,363	.028092 .023879 .020447 .015269 .01179 .008709 .00709 .005986 .005986 .005986	7.947 7.189677 6.504541 5.883219 3.845853 3.20448355 2.747036581 2.15736581 1.748109 1.3735110	5309100 4802482 4344320 39289540 2567628 2139487 1.833723 1.70687 1.604431 1.426114 1.283472 1.166774 .916734	0.1628 .16745 .14305 .12357 .09333 .08404 .07724 .07726 .06641 .0555	2.61914 2.6814 2.5504 2.4255 2.1924 1.7902 1.6574 1.5904 1.4617 1.3222 1.1720 1.1720 1.1720 1.1720 1.1720 1.1720 1.1720 1.1720	0.167600 1.33563 1.335078 0.817348 0.20859 0.006479 0.000658 0.0000452 0.03769 0.015760 0.037328	200 1.3330 1.33330 1.333330 1.333330 1.333330 1.333330 1.33330 1.33330 1.33330
1111111111111111111	10.00 0.00 .40 .60 1.50 2.50 2.76 3.00 3.50 4.50 6.00	10.00 0.00 40 .60 1.00 1.50 2.50 2.76 3.00 4.50 6.00	.700 0.900 .900 .900 .900 .900 .900 .900	16.7 0 2 16.7 0 2	002069 002287 019262 01164433 01164433 0106235 006138 005025 004591 004592 003688 0032688 0032688	8618 7.798224 7.7982297 63811679 52131377 52171377 3476154 2,773526 2,773529 2,18762	5.205237 4.708879 4.258829 3.479333 2.783530 2.3194904 1.850544 1.739490 1.546182 1.391545	0.1512 1.1882 1.1889 1.0815 0.076798 0.06527 0.06527 0.05416 0.05416 0.0446	2,9360 2,75561 2,55834 2,58834 2,08644 1,76654 1,66147 1,58244 1,7827 1,5827 1,	0.12977000 1.2977000 0.74700 0.74700 0.749088550 0.00000 0.004087 0.0040847 0.0040847 0.00441348	1.33331 1.33331 1.33331 1.33331 1.33331 1.33331 1.33331 1.33331 1.33331
1111111111111111111111111	10.00 0.00 .40 .60 1.50 2.50 2.50 3.50 4.50 4.50 1.00	10.00 0.00 .20 .40 .60 1.50 2.00 2.76 3.00 3.50 4.00 4.50 10.00	1.0 00 1.0 00	1 6 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	0.01946 .0164938 .0140988 .0121337 .0067363 .0053484 .0033687 .0033687 .0035687 .0025468	8.6941 2 9 7.88671438 8.667143639 4.20888888 4.20888888 8.50688888 8.50688888 8.50688888 8.50688888 8.50688888 8.50688888 8.50688888 8.50688888 8.50688888 8.50688888 8.50688888 8.50688888 8.50688888 8.50688888 8.506888888 8.50688888888888888888888888888888888888	58022500 58022500 4.749653 3.5095552 2807743 2.807743 2.8076767 1.8666777 1.754667 1.403667 1.076669 1.0766135	0.1.1.1.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0	2,9 4 9 0 2,8 0 4 8 2,6 6 7 9 2,5 3 7 7 2 2,2 9 3 1 4 1,8 7 2 7 1,7 3 2 7 1,6 2 7 9 0 1,5 2 9 0 1,3 8 5 9 9 7 8 0	0.7 4750 0.154000 1.21824 0.953761 0.425283 0.018698 0.005698 0.0003271 0.007952 0.01822447	13331 15330 15330 15332 15332 15332 15332 15332 15332 15332 15332 15332 15332 15332 15332 15332 15332 15332 15332
111111111111111111	2.00 .20 .40 .60 1.00 2.50 2.76 3.50 4.00 4.50 1.00	200 0 200 200 250 0 250 0 250 0 276 300 350 450 0 450 0	1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200	18.262 81.153 81.153 81.153 81.153 81.153 81.153 81.153 81.153 81.153 81.153 81.153 81.153 81.153 81.153	001275 001492 0112693 01086970 007077 005248 004129 003392 0032870 0022500 0022500 001547	7.6.34 50 7 8 6.90 6 9 7 8 6.90 6 9 7 8 6.90 6 9 7 8 6.90 6 9 7 8 6.90 7 8	5628035 5629000 56293902 4668228 3405188 3405188 342704154 1.945797 1.812532 1.712532 1.712532 1.712532 1.712542	0.1221 1127 1043 09648 08414 0724 05557 0557 05500 0446 03316	29040 276381 24994 225993 285993 18448 1.7078 1.6478 1.5976 1.4625 1.4625 1.2077	0.149900 .11721493 .0711930 .04177354 .0005549 .00037118 .00037177 .0012975 .00130686	1.3333333333333333333333333333333333333
1111111111111	0.00 .20 .40 .60 1.50 2.00 2.50 2.76 3.00	0.0 0 .3 0 .4 0 .6 0 1.5 0 2.0 0 2.5 0 3.7 6 3.5 0	1.500 1.500 1.500 1.500 1.500 1.500 1.500 1.500	24.920 24.920 24.920 24.920 24.920 24.920 24.920 24.920 24.920	0.011036 .0093583 .0069285 .0053895 .0053895 .0033684 .0033684 .0023140 .0021443	7.391 4 6 3 6.60 8 1 0 9 4 5.4 7 3 0 8 1 4.4 7 1 7 3 7 2.9 8 1 4 6 1 2.5 5 5 3 8 2.3 7 8 8 2 5 2.2 3 6 0 6 4 1	4.931000 4.462095 4.036737 3.651029 2.386468 1.9886634 1.704653 1.49144914 1.325715	0.1 0.5 0 .0 9 6 7 .0 8 9 3 2 .0 7 2 4 .0 5 5 0 4 .0 4 6 3 .0 4 6 3	2.7190 2.5862 2.43995 2.11146 1.8915 2.15942 1.59423 1.4998	0,146100 1153040 .089405 .089405 .017219 .005587 .0005000 .000000	1.3330 1.3332 1.3332 1.3332 1.3332 1.3332 1.3332 1.3332 1.3332

TABLE	ı.	-	Continued.	TURBULENCE	VELOCITY	AND	SCALE	RATIOS
			0001	TOTAL	12200211	****	00	

				TABLE 1.	[(-3)c	C ()C	T	DE NATIOS			
					$v_1^2 = \frac{\left(q_1^2\right)_N}{\left(\overline{q_1^2}\right)_A^A}$	$v_2^2 = \frac{\left(\overline{q_2^2}\right)^C}{\left(\overline{q_2^2}\right)^A}$, M _B = 0.05			NA.	CA.
N	к	NK	М _С	11	v ₁ ²	v ₂ ²	$\frac{1}{3}(v_1^2 + 2v_2^2)$	v ₁	v 2	$\frac{\binom{L_1}{N}^{C}_{N}}{\binom{L_1}{A}}$	(L ₂) C (L ₂) A
111111111111111111111111111111111111111	0.00 .20 .40 .60 1.00 2.50 2.76 3.50 4.00 4.50 6.00	0.0 0 .2 0 .4 0 .5 0 1.0 0 1.5 0 2.5 0 2.7 6 3.5 0 4.0 0 4.5 0 6.0 0 1.0 0	2.0 0 0 2.0 0 0	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	0.007701 .006502 .0065539 .002719 .002719 .0027162 .001696 .001301 .001037 .001037	5.1 66 7 8 2 4.6 61 7 5 4 0 3.8 11 4 6 7 4 7 2.4 12 3 6 6 5 2 3.0 7 8 11 8 8 0 1.6 5 8 8 5 3 6 2 6 1.1 5 5 8 5 3 8 2 6	3.437200 3.110033 3.8113561 2.81472051 1.663341 1.1386076 1.188041 1.1059520 9.24008 .8316002 .755998 .877999 3.779999 1.370300	0.0878 .0808 .0748 .0695 .0695 .0521 .0462 .03402 .03402 .03402 .03402 .03402 .0288	22700 215537 195531 176551 1.76554 1.57415 1.3346 1.28484 1.17166 1.2470 1.11646 1.9437 1.4330	0.146.000 1.189.05 1.099.4288 0.069.72888 0.015.2530 0.000.03614 0.000.03614 0.026645 0.05664550	1.33 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
111111111111111111	0.00 .40 .60 1.00 2.00 2.76 3.00 4.50 4.50 1.00	0 0.0 0 0.2 0 0.4 0 0.6 0 1.5 0 2.5 0 2.7 6 3.0 0 4.0 0 4.5 0 4.5 0 10.0 0	3.0 0 0 0 3.0 0 0 0 3.0 0 0 0 0 3.0 0 0 0	66666666666666666666666666666666666666	99705655993844998613730913141709676405	20.53 81.55 81.65	1.0198.02 1.122.175.472 1.22.175.472 1.22.175.472 1.22.275.275.275 1.22.275.275 1.22	065581655836658440 00654163108658 0000000000000000000000000000000000	100505905910918 10951460228834602 1132219141840755 11322199887770755 1452219988	123244 096491 09747176 047177 043877985 0000000 00033298 00132832 0132832 0732832	1.333.331 1.333.331 1.333.333.331 1.333.333
111111111111111111111111111111111111111	2.00 2.00 1.00 1.50 2.00 2.50 2.76 3.00 4.50 4.50 4.50	0.00 0.20 0.40 0.60 1.00 2.50 2.76 3.00 4.00 4.50 4.00 1.00	4.0 0 0 4.0 0 0	39.0 4 6 39.0 4 6	0.003844 .003230 .002742 .0023447 .001277 .0009999 .000787 .000589 .000589 .000589 .000467 .000325	0.8114 8 7 7 34 08 8 7 7 34 08 8 7 6 6 6 4 0 8 9 3 1 3 9 2 6 2 2 6 1 0 4 8 5 0 2 1 8 1 3 3 6 7 1 7 8 4 2 8 7 1 4 0 2 3 3 3 0 8 9 2 4 9 2 3 3 3	0.542200 .4904669 .441244 .327476 .262208 .218426 .11743840 .145634 .119147 .093614	0.0 6 2 0 0.5 6 8 4 0.0 5 6 8 4 0.0 4 8 18 7 0.0 3 18 8 1 0.0 2 6 4 18 0.0 2 6 4 18 0.0 2 6 4 18 0.0 2 19 5	0.5170629115573248 0.51706291573244 0.55555444279 0.555555444779	0.170600 11376185 .0834648 .021385 .006676 .00006676 .0000465 .0094682 .009463 .009463 .0094775	11333333333333333333333333333333333333
11111111111111111	0.00 .20 .40 .60 1.00 1.50 2.50 2.76 3.00 4.50 4.50 1.00	0 0.0 0 0.2 0 0.4 0 0.6 0 1.0 0 2.5 0 2.7 6 3.0 0 4.5 0 4.5 0 4.5 0	5.0 0 0 5.0 0 0	40.83555 40.83555 40.83555 40.83555 40.83555 40.83555 40.83555 40.83555 40.83555 40.83555	0.0031647 .0022331 .0022331 .00118395 .001075 .00062664 .00055664 .00035664 .00035664	0.3480 31488443 28488443 285764915 114034967 114034967 112034967 112034 11053486 11053486 11053486 11053486 11053486 11053486 11053486	0.233100 2107839 119783987 117237887 11126122 0.933828 0.0748347 0.062526 0.0511153 0.0401597	0.05635 .051525 .043747 .043747 .02276 .02222 .02129 .011635	917684686492726 863780464450655 5554447743209749 863636443	0.189200 1.1204327 0.994426 0.0547059 0.00077999 0.00005534 0.0119476 0.01946138	1.333333333333333333333333333333333333
111111111111111111	0.00 .20 .60 1.00 2.00 2.50 2.76 3.00 3.50 4.50 4.50 1.00	0 0.0 0 0.4 0 0.6 0 1.5 0 2.0 0 2.7 6 3.0 0 4.5 0 4.5 0 1.0 0	6.0 0 0 6.0 0 0	41111111111111111111111111111111111111	0.027 0.95 0.0228 78 28 28 28 28 28 28 28 28 28 28 28 28 28	0.3827 0.16310 1.14819 1.12919 0.9902 0.66656511 0.052665511 0.052665511 0.036665650 0.044960 0.036665650 0.044960 0.036665650 0.036665650 0.036665650 0.036665650 0.036665650 0.036665650 0.036665650 0.036665650 0.036665650	0.109495430 0.089932957 0.089932957 0.0853430819 0.0447886469 0.033534518 0.0328649933 0.028649933 0.028649933 0.028649933	0.0 5 21 .0 4 7 3 3 8 9 .0 2 3 3 3 9 6 .0 2 2 4 9 3 .0 2 2 4 9 3 .0 2 2 0 3 .0 1 6 7 7 .0 1 2 0	04046 33648017599558 3318165799558 22322299982 2209982	0.21 0988 971 165588 971 1064 952 952 952 0.00 090 666 060 0.00 0556 756 76 0.00 0556 756 76 0.00 0556 056 060 0.00 0566 056 056 056 056 056 056 056 056	1.33331166677 1.33333333311777 1.333333333333333333
11111111111111111	0.00 .40 .60 1.00 2.50 2.50 2.50 3.50 4.50 6.00	0 0.0 0 0.2 0 0.4 0 0.6 0 1.0 0 2.0 0 2.5 0 2.7 6 3.0 0 3.5 0 4.5 0 6.0 0	7.0 0 0 7.0 0 0	4 2.6 11 4 2.6 11	0.02363 .00116073 .00116073 .001096713 .000050398 .00003286 .00003286 .00003287 .0000177	0.0 83766 0.0 75 4995 0.0 75 4995 0.0 610 619 619 619 619 619 619 619 619 619 619	0.056600 0.51124 0.461202 0.41051 0.34066 0.272666 0.19417 0.1869 0.015981 0.015981 0.0123497 0.016937	0.0486 .04401 .03660 .0359 .02229 .01881 .0157 .0157 .0158	0.2279022790287902879028790287902870490287049028704902870490287049097399	0.233200 1.90303 1.53603 1.52402 0.744378 0.011043 0.001155 0.00000 0.008861 0.016869 0.29069 0.29069 1.444416	1,3300 1,3000 1,

TABLE I. - Continued. TURBULENCE VELOCITY AND SCALE RATIOS

2					TABLE 1.	- Continued.		LOCITY AND SCA 7	LE HATIOS			
Section Color Co						$V_1^2 = \frac{\left(q_1^2\right)_N^4}{\left(q_1^2\right)_M^4}$	$v_2^2 = \frac{\left(q_2^2\right)_N^4}{\left(q_2^2\right)_N^4}$, M _B = 0.05			NA	CA
2	N	к	NK	М _С	11	v ₁ ²	ν ₂ ²	$\frac{1}{3}(v_1^2 + 2v_2^2)$	v ₁	v ₂		1 1
Section Control Cont	2	.40	.80	.023	.464	.371594	.419605 .298374	.403602 .258257	.6096 .4219	.6478	2.322131	A 5 2 9
2	5 5	1.00	2.0 0 3.0 0	.023	0.4 6 4 0.4 6 4	.044058 .010725 .004726	167112	.067597	.1036	.3099 .2519	000721	1.1903
40	2	3,00 6,00	6.0 0 1 2.0 0	.023	0.4 6 4 0.4 6 4	.002293	.034306 .011177	0661249	0.7654	1057	.000472 1.389594 1.197477	0.9371
2 150 200 040 0400 0411	2 2	.4 0 .6 0	.8 0 1.2 0	.040	,8 0 0 0,8 0 0	.294319 .150619	.5333812	453981 326704	.5425 .3881	.6440	1066106	1.0042
2	12	1.50 2.00	3.0 0 4.0 0	.040	0.8 0 0 0.8 0 0	.011303	.157891 .106705	.109028	.1063 0661	.3974 .3267	036348	1.1869
8 400 800 1200 800 1200 1200 1200 1200 1200	5 5	6.00	12.00	.040	0.800	0.454888	018756 0866741	012821	0.6745	1370 0.9310	0.685651	1,2744
\$\frac{1}{2}\$\frac{1}{2}\$\frac{1}{1}\$\frac{1}{2}\$\frac	2 2	.60	1.20	.060	1,200	.138272	.556944 362462	.544524 .417387 .257527	.3718	.7463	447473	111804
\$\frac{8}{2}\$ \text{ 400} \tag{0.0000}{1200} \tag{0.0000}{0.0000} \tag{0.0000}{0.00000} \tag{0.0000}{0.00000} \tag{0.0000}{0.00000} \tag{0.0000}{0.00000} \tag{0.00000}{0.00000} \tag{0.00000}{0.000000} \tag{0.00000}{0.00000} \tag{0.00000}{0.00000} \tag{0.00000}{0.00000} \tag{0.00000}{0.00000} \tag{0.00000}{0.00000} \tag{0.00000}{0.00000} \tag{0.00000}{0.00000} \tag{0.00000}{0.00000} \tag{0.00000}{0.000000} \tag{0.00000}{0.000000} \tag{0.00000}{0.000000} \tag{0.00000}{0.000000} \tag{0.00000}{0.000000} \tag{0.000000}{0.000000} \tag{0.000000}{0.0000000} \tag{0.000000}{0.00000000000000} 0.00000000000000000000000000000000000	2 2 2	1.5 0 2.0 0	3.0 0 4.0 0	.060	1,200	.015875	.227308 .155745	156830	0831	.3946	.010207	1.2526
2 150 1500 1000 2000 021046 130159 748055 1451 6013 12900 1290 1290 1290 1290 1290 1290 129		6.0.0	12.00	0100	02.000	0.301743	.027762 1,284528	0.956933	0.5493	11334	359645	12690
2 6.00 1 2.00 1.00 2.00 0.00 0.00 0.00 0.00	5 5	.60 1.00	1.2 0 2.0 0	.100	5.000 5.000	.114627 .049564	.854219 .567447	.607688 .394819	.2226	.9242 .7533	.084846	1,2840
2 6.00 1 2.00 1.00 2.00 0.00 0.00 0.00 0.00	8 8 8	3.00	4.0 0 6.0 0	.100 .100	2.000	.021045 .010767 .004020	.250191 .140033	170383	.1038	.5002	.002362	12946
2 150 300 140 2795 020974 494807 336862 1448 70794 40188 13118 13118 1 1 1 1 1 1 1 1 1 1 1 1	3 3	0.20	12.00 0.40 .80	0.1 4 0	2.000 02.795 2,795	0.214613	1420282	.992892	3716	1.3179 1.1918	.186093	1,3076
2 6.00 12.00 1.40 37.00 0.00 1.00 1.00 1.00 1.00 1.00 1.00	2 2	.60 1.00	1.2 0 2.0 0	.1 4 0 .1 4 0	2,795	.044314	.494807	.530783 .336862	.2105 .1448	.8798 .7034	.048510 .010583	1.3103
2 4.0	2 2	2.0 0 3.0 0	4.0 0 6.0 0	.140	2.795	011600	7 4 7 7 7 7	130063	.0688	.4390	000006	1.3136 1.3159 1.3198
2 1.00	Ź	.40	0.4 0 .8 0	0.180	0 3.5 8 9 3.5 8 9 3 5 8 9	0.160583 .107189	1.794905	1.232333	0.4007 3274 2718	1.4811 1.3397	0.217050 .145422 .093577	
2 3.00 6.00 1.80	2	1.00	2.0 0 3.0 0	180	3.5 8 9 3.5 8 9	.037837	.626 (41	.665644	.1945 .1379	.9897	007083	1,3211 1,3217 1,3223
2 0.00	5	3.0 0 6.0 0	6,0 0 1 2,0 0	.180 180	3.5 6 9	.004745	244550 079748	164615	.0689 .0331	.4945	.000004	1,3232
2 0.00	5	.40	.8 0 1.2 0	.340	6.7 2 4 6.7 2 4	.049196	3,201216 2,618821		.2218 1896	1.7892	.090273	1,3311
2 0.00	3 3	1.5 0 2.0 0	3.0 0 4,0 0	.340	6.7 2 4 6.7 2 4	.011181	1,119031	.749748	.1057		.003430	1,3312
2 4.00 1.00 1.00 1.00 1.00 1.00 1.00 1.00	2	0.20	0.4 0	.340	09.761	0.039476	142708 5315313	.095418 3556701	0.1987	2.3055	011807	1,3314
2 2.00	1 2	.60	1,20	.500	9.7 6 1 9.7 6 1	.021421	3.559077 2.375879	2.379858 1.588082	.1464	1.8866	.043641	1.33851
2	2 2	2.00 3.00	3.0 0 4.0 0	.500	9.7 6 1	.004523	1.056155	.705611 .396802	.0673	1.0277	.000236	1 1.3320
2 1.00	2	6,00 0.20 .40	0.4 C	1.000	9.761	0.014104	193997 7.118320 5.826291	129530 4750248 3887699	1 .1025	2.6680	0.095464	1,3332
2 2.00	1 2	.60 1.00	1.2 0 2.0 0	1.000	18.262		3181827	2122823	.0694	1,7838	.010460	1,3332
2	2 2 2	3.00	4.0 0 6.0 0	1.000	18,262	1.000265	1.414434	.943569 .530726	.0429	.8920 .5097	.000166	1.33338
2 1.00	2	0.2 0 .4 0	0,4 0 .8 0	1.500	24.920	0.008027	6.051848	4.037241 3.304266 2.703048	0.0896	2,4601	0.090082	1,3332
2 3.00 6.00 1.500 24,920 .000159 220871 451130 .0256 .4700 .004501 1.332 .2	2 2	1.00	2.0 0 3.0 0	1.500	24,920	.002787	2705126	1.804346	.0528	1.6447	.009705	1.3333
2 40 80 2000 29.822 .0004200 3.452454 2.303036 .0648 1.6561 .053758 1.3332 2.100 2.000 29.822 .001946 1.885441 1.257609 .0441 1.3731 .009707 1.3332 2.100 2.000 29.822 .001946 1.885441 1.257609 .0441 1.3731 .009707 1.3332 2.200 4.00 2.000 29.822 .001148 1.206929 8.05002 .0339 1.0986 .001699 1.3332 2.000 4.00 2.000 29.822 .000751 8.38145 .559014 .0274 .9155 .000152 1.3332 2.000 4.00 2.000 29.822 .000751 8.38145 .559014 .0274 .9155 .000152 1.3332 2.000 1.200 29.822 .000138 4.71455 3.14433 .0197 .6866 .0000152 1.3332 2.000 1.200 2.000 29.822 .000138 4.71455 3.14433 .0197 .6866 .000011 1.3332 2.000 4.00 3.000 35.866 .0003612 1.681025 1.121887 .00601 1.2965 .009664 2.13332 2.000 4.00 3.000 35.866 .002690 1.375906 .918167 .0519 1.1730 .058046 1.3331 2.100 2.003 3.000 35.866 .002690 1.375906 .918167 .0519 1.1730 .058046 1.3331 2.100 2.003 3.000 35.866 .000244 1.125601 .751082 .0452 1.0609 .03877 1.3331 2.100 2.003 3.000 35.866 .000244 1.125601 .751082 .0452 1.0609 .03877 1.3331 2.100 2.003 3.000 35.866 .000244 1.125601 .751082 .0452 1.0609 .03877 1.3331 2.100 2.003 3.000 35.866 .000244 1.125601 .751082 .0452 1.0609 .03877 1.3331 2.100 2.003 3.000 35.866 .000244 1.125601 .751082 .0452 1.0609 .03877 1.3331 2.100 2.003 3.000 35.866 .000244 1.125601 .751082 .0452 1.0609 .03877 1.3331 2.100 2.003 3.000 35.866 .000244 1.135601 .751082 .0452 1.0609 .03877 1.3331 2.100 2.003 3.000 35.866 .000244 1.135601 .751082 .0452 1.0609 .03877 1.3331 2.100 2.003 3.000 35.866 .000244 1.135601 .751082 .0452 1.0609 .03877 1.3331 2.100 2.003 3.000 35.866 .000244 1.135601 .351082 .000244 1.13580 .000244	2 2	3.0 0 6.0 0	6.0 0 1 2,0 0	1.500	24.920	.000556	.676417	.451130 147300	.0236	.8224	.000001	1,3332
2 1,50 3,00 2,000 29,822 .0001148 1,206929 8,005002 .0339 1,0986 .000159 1,3332 2 3,00 4,00 2,000 29,822 .000751 8,38145 5,359014 .0274 9,155 .000153 1,3332 2 3,00 4,00 2,000 29,822 .000388 4,711455 3,14433 .0195 .6866 .000152 1,3332 2 6,00 12,00 3,000 35,866 .00061 1,1415 9,00 1,1	5 5 5	.60	.8 0 1,2 0	2.000	29.822	.004200	3.452454	2.303036	.0648	1.6806	.053758	1.3332
2 5.00 12.00 29.82 2 .000181 1.33944 102632 0.10195 3.3949 .000181 1.3332 2 .000181 1.3328 2 .000181 1.3328 2 .000181 1.3328 2 .000181 1.3328 2 .000181 1.30081 2 .000181 1.3008	5 5	1.50	3.0 0 4.0 0	2.000	29,822	.001946	1.206929	.805002 .559014	.0339	10986	.001699	
2 40 80 33000 35866 .002694 1.375906 .751082 .0319 1.1750 .031879 1.3731 2 1.00 2.00 3.000 35866 .001229 .751403 .501345 .0351 .86668 .0106279 1.3331 2 1.50 3.00 3.000 35866 .001229 .751403 .501345 .0351 .86668 .0106279 1.3331 2 2.00 4.00 3.000 358666 .000719 .80996 .320904 .0216 .5779 .0001627 1.3331 2 2.00 4.00 3.000 35866 .000240 .167889 .0155 .84777 .0000711 .3331 2 2.00 4.00 3.000 35866 .000240 .167889 .0155 .84777 .0000711 .3331 2 2.00 4.00 3.000 35866 .000223	3 S	6.00	1 2.0 0 0.4 0	3.000	29.822 35.866	0.00388	1,681025	102666 1121887	0.0601	12965	004551	1.3332
2 40 80 5,000 40,835 .001623 .233171 .155988 .04403 .4829 .074199 1.3328 2 1.00 2.00 5,000 40,835 .001209 190752 1.257571 .0348 .4368 .044197 1.3328 2 1.00 2.00 5,000 40,835 .000704 1.27337 .085126 .0265 .35688 .014318 1.3328 2 2.00 4.00 5,000 40,835 .000400 .015312 .085126 .0265 .35688 .014318 1.3328 2 2.00 4.00 5,000 40,835 .000254 .056605 .037822 .01552 .2399 4 .0002461 1.3328 2 2.00 4.00 5,000 40,835 .000254 .056605 .037822 .01552 .2399 4 .0002461 1.3328 2 2.00 12.00 5,000 40,835 .000256 .015840 .021866 .0152 .0152 .2399 4 .0002461 1.3328 2 2.00 12.00 5,000 40,835 .000126 .015840 .021866 .0168 .0200 .00056 .13326 2 2.00 12.00 40,835 .000256 .	2 2	1,00	1.2 0 2.0 0	3.000	35,866 35,866	.002690	1.375906 1.125601 751403	918167	0452	1.0609	.010629	1,3331
2 40 80 5,000 40,835 .001623 .233171 .155988 .04403 .4829 .074199 1.3328 2 1.00 2.00 5,000 40,835 .001209 190752 1.257571 .0348 .4368 .044197 1.3328 2 1.00 2.00 5,000 40,835 .000704 1.27337 .085126 .0265 .35688 .014318 1.3328 2 2.00 4.00 5,000 40,835 .000400 .015312 .085126 .0265 .35688 .014318 1.3328 2 2.00 4.00 5,000 40,835 .000254 .056605 .037822 .01552 .2399 4 .0002461 1.3328 2 2.00 4.00 5,000 40,835 .000254 .056605 .037822 .01552 .2399 4 .0002461 1.3328 2 2.00 12.00 5,000 40,835 .000256 .015840 .021866 .0152 .0152 .2399 4 .0002461 1.3328 2 2.00 12.00 5,000 40,835 .000126 .015840 .021866 .0168 .0200 .00056 .13326 2 2.00 12.00 40,835 .000256 .	2 2	1.5 0 2,0 0 3.0 0	3.0 0 4,0 0 6,0 0	3,000 3,000 3,000	35,866 35,866 35,866	.000468	.334025	125339	.0216	.4335	.000169	1.3331
2	2	6,00	040 .80	5.000	35,866 40.835 40.835	0.000067	0.284879	0190663 .155988	0.0472	0.5337	0.120618 .074199	1.3385
2 .60 120 7.000 42.611 .001132 .056072 .037739 .0337 .2366 .377666 .1.3702 .2 .60 120 7.000 42.611 .000820 .045870 .030854 .0286 .2142 .059825 1.3308	2 2	1,00	2.00	5.000	4 0.8 3 5	.001209	.190752 .127337 .081512	127571 085126 054475	.0265	.4368		1.3325 1.3325 1.3325
2 .60 120 7.000 42.611 .001132 .056072 .037739 .0337 .2366 .377666 .1.3702 .2 .60 120 7.000 42.611 .000820 .045870 .030854 .0286 .2142 .059825 1.3308	2	2.0 0 3.0 0	4.0 0	5.000	4 0.8 3 5 4 0.8 3 5	.000254	056605	.037822 .021269 .006942	0159	1 1784		1.3325 1.3325 1.3326
\$ 1.00 2.00 7.000 42.611 .000456 .030620 .020566 .0214 .1750 .020278 13303	5	.40	,80	7,000	4 2.6 1 1	.001132	.056072	0.046208		.2368	0.59825	
2 1.50 3.00 7.000 42.611 .000248 .019600 .01914 .0124 .1167 .000367 1.3304 .01610 .009124 .0124 .1167 .000367 1.3304	00000	1.00 1.50	2.0 0	7.000	4 2.6 1 1	.000456	.030620 .019600 .013610 .007655	.020565	0124	1 .1400	020278	1.3302 1.3303 1.3304 1.3305
2 200 400 7000 42611 0000153 013610 009124 0124 1167 000367 13304 2 300 600 7000 42611 000072 007655 005127 0085 0875 000002 13305 2 600 1200 7000 42611 000018 002499 001672 0042 0500 013846 13307	8	3.00	6.00	7.000	42.611	.000072	.007655	.005127	,0085	0875	.000002	1,3305 1,3307

TABLE I. - Continued. TURBULENCE VELOCITY AND SCALE RATIOS

					TADDS 1.	г .	TORDOLISMOE VE	ראג וווסטבו ר	DE RAIIOS			
						$v_1^2 \equiv \frac{(\overline{q_1^2})_N^2}{(\overline{q_1^2})_N^4}$	$v_2^2 = \frac{\left(\overline{q_2^2}\right)_N^C}{\left(\overline{q_2^2}\right)_N^A}$, M _B = 0.05				~
						$(q_1^2)^n$	$(q_2^2)^n$				MA NA	A
	N	к	NK	M _C	11	v ₁ ²	v ₂ ²	$\frac{1}{3}(v_1^2 + 2v_2^2)$	v ₁	v ₂	$\frac{\left(L_1\right)_N^C}{\left(L_1\right)^A}$	$\frac{\left(L_{2}\right)_{N}^{C}}{\left(L_{2}\right)_{N}^{A}}$
	3	0.20 .40 .60 1.00 1.50	0.6 0 1.2 0 1.8 0 3.0 0 4.5 0	0.0 2 3 .0 2 3 .0 2 3 .0 2 3	0.4 6 4 .4 6 4 .4 6 4 .4 6 4	0.5 4 0 0 4 0 .179 0 7 1 .0 6 2 6 5 8 .0 1 0 8 2 9	0.506067 .298411 .191382 .090657	0,517391 ,258631 ,148474 ,064048 ,029982	0.7 349 .4232 .2503 .1041 .0556	0.7114 .5463 .4375 .3011 .2084	2.585687 2.332176 1.969100 .932920 .108462 .002965	0.6795 .8533 .9845 1.1335 1.2119 1.2467
1	3 3 3	2.00	6.0 0	.023	.464	.001602	.024431	.016821	0400 0256 0.6439	.1563 .1003 0.7806	1,134084	0.9726
	3 3 3 3	0.2 0 .4 0 .6 0 1.0 0	0.6 0 1.2 0 1.8 0 3.0 0	0.0 4 0 .0 4 0 .0 4 0	0.8 0 0 .8 0 0 .8 0 0	0.414559 .150915 .057997 .010863	0,609296 .414814 .290588 .149045	0.544384 ,326848 ,213058 ,102984	.3885 .2408 1042	.6441 .5391 .3861	931719 .716250 .313094 .046378	1.0 5 7 9 1.1 1 7 4 1.1 8 8 2 1,2 3 3 5
	3 3 3	1.5 0 2.0 0 3.0 0	4.5 0 6.0 0 9.0 0	.040	.800 .800 .008.	.002433 .000948 .000297	.073531 .041722 .017244	.049832 .028130 .011595 0.627824	.0493 .0308 .0172	.2712 .2043 .1313	.001686 .000001 0.625219	1.3581 1.3842 1.1468
	3 3 3	0.20	0.6 0 1.2 0 1.8 0	0.060 .060	01,200 1,200 1,200	0.334281 .138245 .061227	0.774595 .557192 .403982	289731	0.5782 .3718 .2474 .1221	0.8 8 0 1 .7 4 6 5 .6 3 5 6 .4 6 3 4	452149 301609 .101467	1.1806
	3 3	1.00 1.50 2.00	3.0 0 4.5 0 6.0 0	.060	1,200 1,200 1,200	.014901 .003837 .001410	214731 107935 061748 025715	.073236 .041635 .017259	.0619 .0375	.3285 .2485	.013076	1,2 5 6 3 1,2 5 9 7 1,2 7 4 3 1,2 9 0 9 1,3 7 1 5
-	3 3 3 3	3.0 0 0.2 0 .4 0	9.0 0 0.6 0 1.2 0	0.100	1.200 02.000 2.000	0.233820 .114535 .060266	1159982 .854734 .630013	0.851261 .608001 .440097	0.4835 .3384 .2455	.1604 1,0770 ,9245 .7937	0.322197 .196721 .110452	1,2778
	3 3	.60 1.00 1.50	1.8 0 3.0 0 4.5 0	.100 .100	2.000	.019742 .006456 .002674	.341681 .174120 .100394	234368 118232 067821	.1405 .0804 .0517	.5845 .4173 .3169	.027607 .002801 .000096	1,2900 1,2965 1,3013
-	3 3 3	2.00 3.00	6.0 0 9.0 0 0,6 0	,100 ,100 0.140	2.000 2.000 02.795	0.171388	.042144 1.570760 1,161718	028329 1104303 805110	,0265 0.4140 .3031	.2053 1.2533 1.0778	0.224697 .125338	1,3077 1,3070 1,3086 1,3100
	3 3 3	.40 .60 1.00	1.2 0 1.8 0 3.0 0	.140 .140 .140	2.7 9 5 2.7 9 5 2.7 9 5	.091893 .0526 07 .019738 .007263	.858724 .467611 .239110	,590018 .318320	.2294 .1405 .0852	.9267 .6838 .4890	.064681 .014115 .001273	1.3121
	3 3	1.50 2.00 3.00	4.5 0 6.0 0 9.0 0	.140 .140 .140	2.7 9 5 2.7 9 5 2.7 9 5	.003261	.138196 .058187	161828 .093218 .039106 1366534	.0571 .0307 0.3614	.3717 .2412 1.4087	000040	1.3159 1.3184 1.3200
	3 3 3	0.2 0 .4 0 .6 0	0.6 0 1.2 0 1.8 0	0,180 .180 .180	0 3.5 8 9 3.5 8 9 3.5 8 9	0.130623 .073861 .044337 .017917	1.468924 1.086540 .592291	1,003903 739139 400833	.2718 .2106	1.2120	.094572 .046545 .009430	1.3205
	3 3	1.00 1.50 2.00	3,0 0 4,5 0 6,0 0	.180 .180	3.5 8 9 3.5 8 9 3.5 8 9 3.5 8 9	.007045 .003322 .001027	.303168 .175357 .073919	204461 ,118012 ,049621	.0839 .0576 .0320	,5506 ,4188 ,2719 1,8818	.000796 .000024 .000000	1,3225 1,3231 1,3242
	3 3	3.00 0.20 .40	9.0 0 0.6 0 1.2 0	0.3 4 0 .3 4 0 .3 4 0	0 6.7 2 4 6.7 2 4 6.7 2 4	0.058120 .035932 .023271	3.538875 2.620464 1.938943	2.378623 1.758954 1.300385	0.2411 ,1896 ,1525	1.6188	0.114493 .055386 .025266	1,3311 1,3311 1,3311 1,3312
	3333	1.00 1.50	1,8 0 3,0 0 4,5 0	.340 .340 .340	6.7 2 4 6.7 2 4 6.7 2 4	.010561 .004615 .002363	1.057512 541593 313411	.708529 .362600 .209728	.1028 .0679 .0486	1.0284 .7359 .5598	004558 .000346 .000010 .000000	1.3312 1.3313 1.3325 1.3325
	3	2.0 0 3.0 0	6,0 0 9,0 0 0,6 0	0.500	6.7 2 4 0 9.7 6 1 9.7 6 1	0.033565 .021424	132212 4.809388 3.561311 2.635133	088417 3217447 2381348	0.1832 1464	3636 21930 18871	0.094079	1,3325
	3	.40 .60 1.00	1,2 0 1,8 0 3.0 0 4,5 0	.500 .500	9.7 6 1 9.7 6 1 9.7 6 1	.014238 .006716	736096	1,761502 .960408 .491744	.1193 .0819 .0551	1,6233 1,1989 .8580	.019596 .003402 .000249	1,3325 1,3325 1,3326 1,3326
	3 3 3	1.50 2.00 3.00	6.0 0 9.0 0	.500 .500 .500	9.7 61 9.7 61 18.2 62	.001601 .000585	425979 179708 6.440788	284520 120000 4297906	.0400 .0242 0.1102	.6527 4239 25379	000000	1,3336 1,3332 1,3332
	3 3	.40	0.6 0 1,2 0 1,8 0 3.0 0	1.000	18.262 18.262 18.262	.008001	4.769367 3.529023 1.924808	3,182245 2,354499 1,284095	.0894 .0738 .0516	2.1839 18786 13874	.033725 .014620 .002447 .000174	1.3332 1.3332 1.3332
	3 3 3 3	1.00 1.50 2.00 3.00	4.5 0 6.0 0 9.0 0	1.000 1.000 1.000	18,262 18,262 18,262	.001248 .000675 .000257	.985804 .570488 .240674	.657619 .380550 .160535	.0353 .0260 .0160	9929 7553 4906 23400	000000	1,3332 1,3332 1,3332 1,3332
	3 3	0.20	0.6 0 1,2 0 1.8 0	1.500 1.500 1.500	2 4.9 2 0 2 4.9 2 0 2 4.9 2 0	0.006930 .004599 .003152	5.475824 4.054817 3.000303	3.652859 2.704744 2.001253	0.0832 .0678 .0561 .0394	2.0137 1.7321 1.2792	.031508 .013584 .002256	1,3332 1,3332 1,3332
	3 3	1.00 1.50 2.00	3.0 0 4.5 0 6.0 0	1.500 1.500 1.500	2 4.9 2 0 2 4.9 2 0 2 4.9 2 0	.001554 .000732 .000398	1636434 838111 485018	1.091474 .558985 .323478	0271 0199 0124	9155 ,6964 ,4523	.000159 .000004	1.3332
	3 3 3	3,00 0,20 .40	9,0 0 0.6 0 1 2 0	2.0 0 0 2.0 0 0	2 4.9 2 0 2 9.8 2 2 2 9.8 2 2	0.00153 0.004838 .003211	204616 3.816584 2.826159	2.546002 1.885176 1.394850	0.0696	1,9536 1,6811 1,4461	0.069932 031513 .013587	1,3332 1,3332 1,3332 1,3332
	3 3 3	1.00 1.50	1.8 0 3.0 0 4.5 0	5.000 5.000 5.000	29.822	.002200	2.091175 1.140575 .584153 .338052	.760745 .389606 .225460	.0329	10680 .7643 .5814	.002256	1,3332 1,3332 1,3332
	3 3	2.0 0 3,0 0 0.2 0	6.0 0 9.0 0 0.6 0	2.0 0 0 2.0 0 0 3.0 0 0	2 9.8 2 2 2 9.8 2 2 3 5.8 6 6	0.00107	1.521022	.095112 1.015051 .751554	0.0557	3776 1,2333 1,0613	0.075272 0.075272 0.034216	1,3332 1,3331 1,3331
	3 3	.60 1.00	1,2 0 1,8 0 3,0 0	3.0 0 0 3.0 0 0 3.0 0 0	35.866 35.866 35.866	.002045	1.1 26 3 0 8 .8 3 3 3 9 5 .4 5 4 5 5 3 .2 3 2 8 0 2	556060	.0373	.9129 .6742 .4825	.014851 .002490	1,3 3 3 1 1,3 3 3 1 1,3 3 3 1
	3 3 3	2.00 3.00	4.5 0 6.0 0 9.0 0	3.0 0 0 3.0 0 0 3.0 0 0	35.866 35.866 35.866	.000318 .000171 .000065	.234724 .056836	.089873 .037913	.0131 .0081	,3670 ,2384	000000	1,3331 1,3331 1,3325
	3	0.20	0.6 0 1.2 0 1.8 0	5.000 5.000 5.000	4 0.8 3 5 4 0.8 3 5 4 0.8 3 5	.001209	.190872	127651 094422 051480	.0348 .0283 .0194	.4369 .3758 .2775	.044644	1,3325
	3 3 3 3	1.00 1.50 2.00	3.0 0 4.5 0 6.0 0	5.000 5.000 5.000	4 0.8 3 5 4 0.8 3 5 4 0.8 3 5 4 0.8 3 5	000171	.039452	026358	.0131 .0095	1986 1511 0981	000254	1,3325 1,3325 1,3325
	3 3 3	0.2 0 -4 0	9.0 0 0.6 0 1.2 0	7.000 7.000 7.000	4 2.6 1 1 4 2.6 1 1 4 2.6 1 1	0.001344	0.061987 .045899	0.041772 030873 022816	0,0367 ,0286 ,0229	0,2490 ,2142 ,1843	0.123296 .060441 .027877	1.3301 1.3302 1.3302
	3	1.00	1.8 0 3.0 0	7.000	42,611	.000235	.018522	012426	0153	1361		1,3303

$\left(\overline{q_1^2}\right)_{N}^{C}$	$= \frac{\left(\overline{q_2^2}\right)_N^C}{\left(\overline{q_2^2}\right)_A^A}, M_B = 0.05$
$v_1 = \overline{\left(\overline{q_1}^2\right)^A}, v_2^{-1}$	$(\overline{q_2^2})^A$, $M_B = 0.05$

					$v_1^2 \equiv \overline{\left(q_1^2\right)}$	\tilde{A} , $V_2^2 \equiv \overline{\left(q_2^2\right)}$	Ä, M _B ≈ 0.05			N. N.	CA
N	к	NK	M _C	11	v ₁ ²	v ₂ ²	$\frac{1}{3}(v_1^2 + 2v_2^2)$	v ₁	v ₂	(L ₁) C	(r ⁵) ^N _C
-	0,20	200	-				ļ -	ļ		(L ₁) A	(L2) A
4	.60	0.8 0 1,6 0 2.4 0	0.023	0.4 6 4 .4 6 4	0.372531 .088571 .024446	0.419630 .220316 .129723	0.403930 .176401 .094631	0.6104 .2976 1564	0.6478 .4694 .3602	2.511752 2.112971 1.506345	0.7415 ,9461 1.0754
4	1.00	4.0 0 6.0 0	.023	.4 6 4 .4 6 4	.004133	.052064	.036087	.0643	.2282	.316765 .010418	1.1940
4	2.0 0 3.0 0 0.2 0	8.0 0 1 2.0 0 0 0.8 0	.023 .023	.4 6 4 .4 6 4 0,8 0 0	.000627 .000196 0.294622	.009659 .003004 0.533822	.006648 .002068	.0250 .0140 0.5428	.0983 .0548	.000076 .000000 1,069313	1,2719 1,2939 1,0045
4	.40 .60	1.6 0 2.4 0	.040	800	.079295	.326488 .207318	.24409C	.2816	.5714	.794642	1.1003
4 4	1.00 1.50 2.00	4.0 0 6.0 0 8.0 0	.040	0 0 8. 0 0 8. 0 0 8.	.003558	.087652 .034873 .016564	.059621 .023793 .011139	.0596	.2961	.123891	1.2223
4	3.00 0.20	1200	0,060	1,200	0.247292	0.693267	0.544608	.0171 .0144 0.4973	.1287 .0718 0.8326	0.566333	1,2782 1,2992 1,1594
4 4	.40 .60 1,00	1,6 0 2.4 0	.060	1,200	.079644	.449581	,326269	.2822	.6705 .5428	.351702	1.1977
4	1.50	4,0 0 6.0 0 8.0 0	.060 .060	1,200 1,200 1,200	.005464	,128129 ,051638 ,024658	.087241 .034808 .016559	.0739 .0339 .0190	.3580 .2272 .1570	.035861	1,2534 1,2744 1,3870
4	3.00 0.20	12.00	0.100	2.000	0.182755	.024658 .007718	0.759380	0.4275	1.0236	0.276230	1,3011
4 4	.40 .60 1.00	1,6 0 2,4 0 4,0 0	.100 .100	2.0 0 0 2.0 0 0	.074048 .033598 .008663	.697804 .464998 .205972	.489885 .321198 .140202	.2721 .1833 .0931	.8353 .6819 .4538	.136356 .059130 .008154	1,2812 1,2867 1,2945
4	1.50 2.00	6.0 0 8.0 0	100	2.000	,002214	.083972	056719	.0471	.2898	.000340	1,3011
4 4	3.00 0.20 .40	1 2.0 0 · 0 0.8 0 1,6 0	0.1 4 0 .1 4 0	2.000 2.795 2.795	.000141 0.138086 .062928	.012706 1.420634 .950311	.008518 0.993118 .654517	.0119 0.3716 .2509	.1127 1.1919 .9748	.000000 0.186881 .082020	1,3121 1,3076 1,3095
4 4	1.00	2.4 0 4.0 0	.140	2.7 9 5 2.7 9 5	.031611	.635245 .282570	.434034 .191528 .077965	.1778	.7970 .5316	.032127	1.3111 1.3135 1.3158
4 4	1.5 0 2.0 0 3.0 0	6.0 0 8.0 0 1 2.0 0	.140 .140 .140	2,7 9 5 2,7 9 5 2,7 9 5	.002721 .000996 .000207	115587 055665 017577	.037442	.0522 ,0316 ,0144	.3400 ,2359 ,1326	.000142	1.3158 1.3176 1.3203
4	0.2 0 -4 0	1,60	.180	3.5 8 9 3.5 8 9	0.107175	1,795354 1,202174	.011787 1.232627 .818868	0.3274	1.3399	0.146030	1,3202
4 4	1.00 1.50	2.4 0 4.0 0 6.0 0	.180 .180 .180	3.5 8 9 3.5 8 9 3.5 8 9	.027760	,804234 ,358159 ,146665	.545410 .241772 .098672	.1666 .0948 .0518	8968 5985 3830	.022187 .002434 .000087	1.3214 1.3222 1.3231
4	2.0 0 3.0 0	8.00 12.00	.180	3.5 8 9 3.5 8 9	.001072	.070690 .022347 3.202019	.047484	.0327 .0155	.2659 .1495 1,7894	.000001 .000000	1.3238
4 4	0.2 0 .4 0	0 0,8 0 1,6 0 2,4 0	0,340	6.7 2 4 6.7 2 4 6.7 2 4	0.049196 .026790 .015537	3.202019 2.145072 1.435571	2.151078 1.438978 .962226	0.2 2 1 8 .1 6 3 7 .1 2 4 6	1.4646	0.090638 .033291 .011294	1,3311 1,3311 1,3311
4	1.00 1.50	4.0 0 6.0 0	,340 ,340 ,340 ,340	6.7 2 4	.005717	.639715 .262123	.428382 .175409	.0756 .0445	11982 7998 ,5120	.001091	1.3312
4 4	2.00 3.00	8.0 0 1 2.0 0 0 0.8 0	340	6.7 2 4 6.7 2 4 9.7 6 1	.000837 .000215 0.028736	.126404 .039992 4.351619	.084549 .026733 2.910658	.0289 .0147 0.1695	.3555 .2000 2.0861	.000000 .000000 0.073637	1.3313 1.3314 1.3325
4 4	.60	1.60 2.40	.500	9.7 6 1 9.7 6 1	.016262	2.915262 1.951048	1.948929 1.303936	1275 .0985	1.7074	.026025	1,3325
4 4	1.00 1.50 2.00	4.0 0 6.0 0 8.0 0	.500 .500	9.7 6 1 9.7 6 1 9.7 6 1	.003726 .001342 .000585	.869446 .356268 .171810	.580873 .237959 .114735	.0610 .0366 .0242	.9324 .5969 .4145	.000795 .000024 .000000	1.3326 1.3326 1.3326
4	0,2 0 0,2 0	1200 0080	1.000	9.7 6 1 1 8.2 6 2	.000158 0.010515	.054361 5.827744	.036293 3.888668	0.1025	2,4141	0.057497	1.3326
4 4	.40 .60 1.00	1.6 0 2.4 0 4.0 0	1.000 1,000 1,000	1 8.2 6 2 1 8.2 6 2 1 8.2 6 2	.006181 .003795 .001504	3.904175 2.612889 1.164390	2,604843 1,743191 ,776761	0786 0616 0388	1.9759 1.6164 1.0791	.019565 .006269 .000563	1,3332 1,3332 1,3332
4	1,50 2,00	6.0 0 8.0 0	1.000	18.262 18.262	.000565	.477129 .230097	.318275 153483	.0238	.6907 .4797	.000016	1,3332
4 4	3.00 0.20 .40	1,2.0 0 0.8 0 1.6 0	1,000 1,500 1,500	2 4.9 2 0 2 4.9 2 0	.000072 0.006017 .003566	.072804 4.954627 3.319249	048560 3.305090 2.214021	.0085 0.0776 .0597	.2698 2.2259 1.8219	.000000 0.053962 .018209	1,3332
4	.60 1.00	2.4 0 4.0 0	1.500 1.500	2 4.9 2 0 2 4.9 2 0	.002203	2.221425	.660257	.0469 .0298	1.4904	.005799	1,3332 1,3332 1,3332
4	1.5 0 2.0 0 3.0 0	6,0 0 8,0 0 1 2,0 0	1.500 1.500 1.500	24.920 24.920 24.920	.000334 .000151 .000043	405646 195624	.270542	.0183	.6369 .4423	.000015	1,3332
4 4	0.2 0 .4 0	0.8 0 1.6 0	2.000	29.822	0.004201	.061896 3.453316 2.313477	041279 2303611 1543148	0.0648	,2488 1.8583 1.5210	.000000 0.053970 .018212	1,3332 1,3332 1,3332
4	.60 1.00 1.50	2.4 0 4.0 0 6.0 0	2.000 2.000	2 9.8 2 2 2 9.8 2 2 2 9.8 2 2	.001538 .000619 .000233	1.548307 .689977 .282730	1.032717 .460191 .188564	.0392 .0249 .0153	1.2443 .8306 .5317	.005800 .000513	1,3332 1,3332 1,3332
4	3.00 3.00	8.0 0 1 2.0 0 0.8 0	2,000 2,000	29.822 29.822	.000105 .000030 0.002690	.136348 .043141	.090933	.0103	.3693	.000000 .000000 0.058276	1,3332 1,3332 1,3331
4 4	.40 .60	1.6 0 2.4 0	3.0 0 0 3.0 0 0 3.0 0 0	3 5.8 6 6 3 5.8 6 6 3 5.8 6 6	.001578	1.376249 .921989 .617046	0.918396 .615185 .411686	0.0519 .0397 .0311	1.1731 .9602 .7855	0.058276 .019867 .006374	1.3331
4 4 4	1.00 1.50	4,0 0 6,0 0 8,0 0	3.000	3 5.8 6 6 3 5.8 6 6	.000386	.617046 .274976 .112676	.411686 .183446 .075165	.0196	.5244	.000569	1,3331 1,3331 1,3331 1,3331
4	2.00 3.00 0.20	1200	3.0 0 0 3.0 0 0 5.0 0 0	3 5.8 6 6 3 5.8 6 6 4 0.8 3 5	.000064 .000018 0.001623	.054338 .017193 0.233229	.036247 .011468 0156027	.0080 .0043	.2331 .1311 0.4829	.000000	1.3338
4 4	.40 .60 1.00	1.6 0 2.4 0 4.0 0	5.000	4 0.8 3 5 4 0.8 3 5	.000917	.156246	.104470	.0303	.3953	026381	1.3325 1.3325 1.3325
4	1.5 0 2.0 0	6.0 0 8.0 0	5.0 0 0 5.0 0 0 5.0 0 0	4 0.8 3 5 4 0.8 3 5 4 0.8 3 5	.000209	.046599	.031136 .012755 .006150	.0145 .0087 .0057	.2159 .1382 .0960	.000808	1,3325 1,3325 1,3325
4 4	0.20	0.8 0	7.000	4 2.6 1 1	0.000009	0.03914	0.01945 0.03776B	0.030	0.2368	0.098065	13326
4 4	.40 .60 1.00	1.6 0 2.4 0 4.0 0	7.000 7.000 7.000	4 2.6 1 1 4 2.6 1 1 4 2.6 1 1	.000607 .000348 .000126	.037572 .025144 .011204	.025250 .016879 .007512	.0246 .0186 .0112	.1938 .1586 .1059	.036606 .012576 .001237	1,3301 1,3302 1,3303 1,3303
4 4	1.5 0 2.0 0 3.0 0	6.0 0 8.0 0	7.000	4 2.6 1 1 4 2.6 1 1	.000043	.004591	.003075 .001482 .000468	.0065	.0678	.000039	1.3304
<u> </u>	2,00	1 2,0 0	7.000	4 2.6 1 1	.000005	.000700	.000468	.0021	.0265	.000000	1.3307

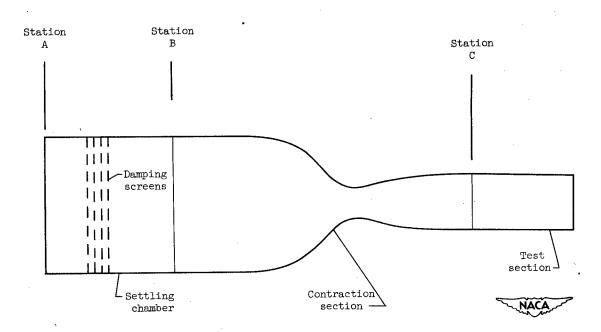


Figure 1. - Configuration treated in analysis.

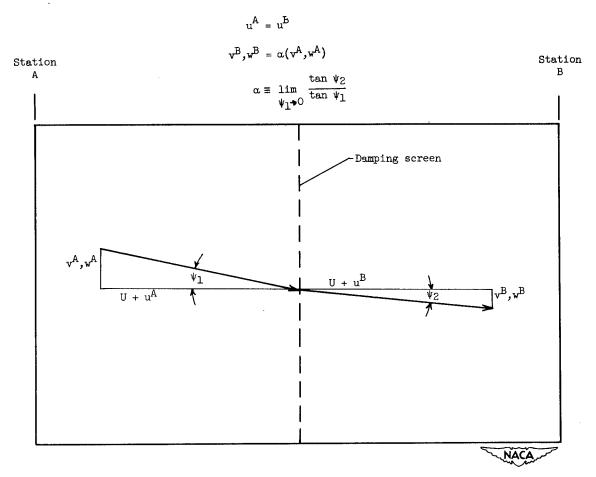
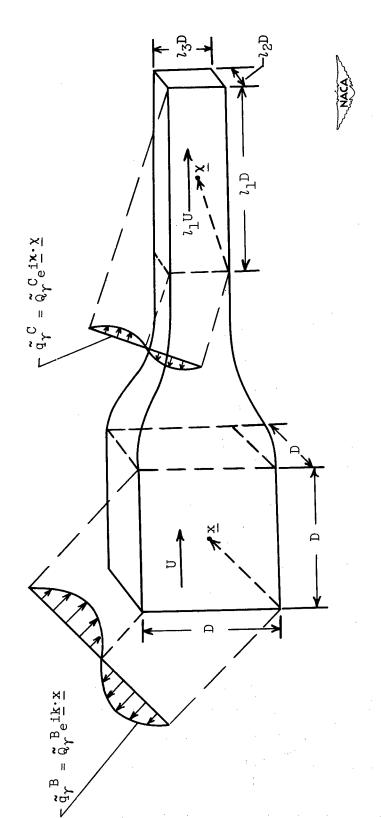


Figure 2. - Action of damping screen on components of combined turbulent and induced velocities at screen.

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- Typical fluid-element- and plane-wave distortions resulting from stream convergence. Figure 3.



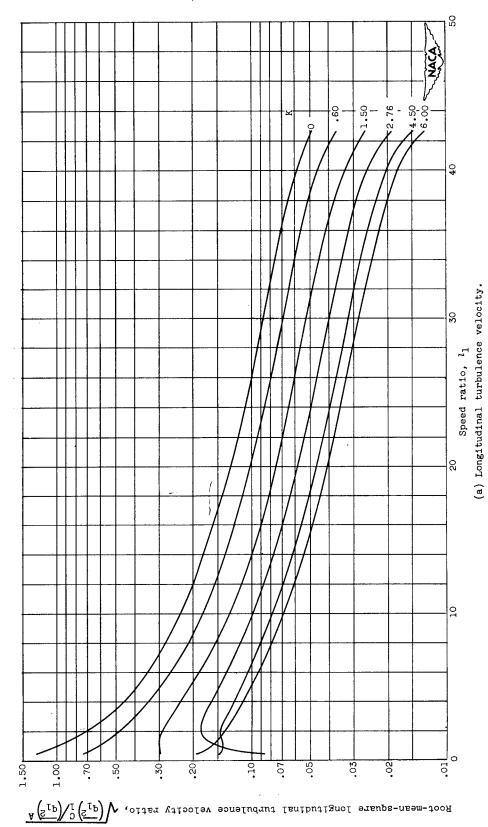


Figure 4. - Variation of root-mean-square turbulence velocity ratio with speed ratio (M_B of 0.05) and screen pressure-drop coef-ficient K in absence of turbulence decay for single-screen-axisymmetric-contraction configurations with upstream isotropic turbulence.

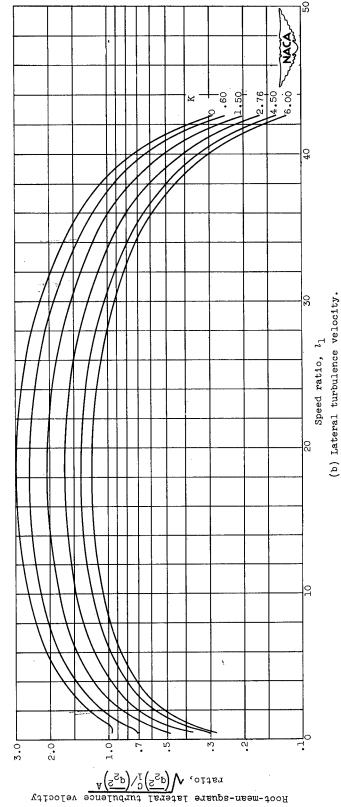


Figure 4. - Concluded. Variation of root-mean-square turbulence velocity ratio with speed ratio (M_B of 0.05) and screen pressure-drop coefficient. K in absence of turbulence decay for single-screen-axisymmetric-contraction configurations with upstream isotropic turbulence.



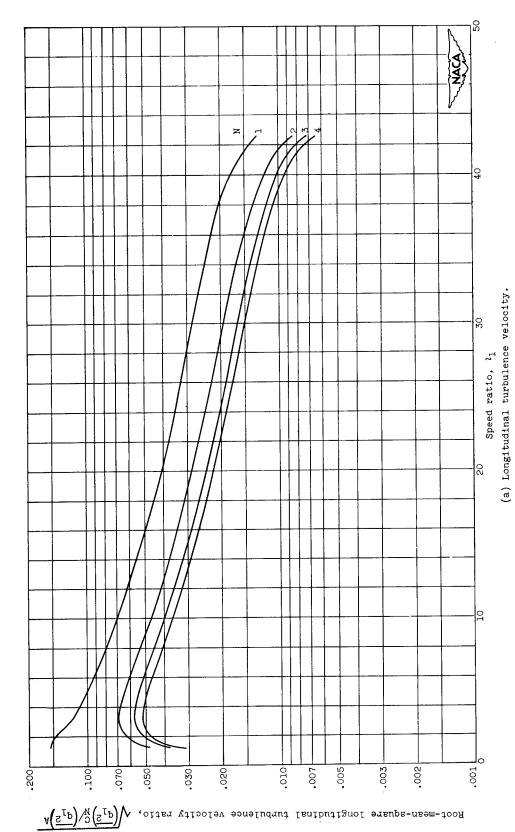


Figure 5. - Effect of multiple screens N and speed ratio (M_B of 0.05) on root-mean-square turbulence velocity ratio in absence of turbulence decay for screen-axisymmetric-contraction configurations with upstream isotropic turbulence and constant screen losses. Over-all screen pressure-drop coefficient, NK, 6.

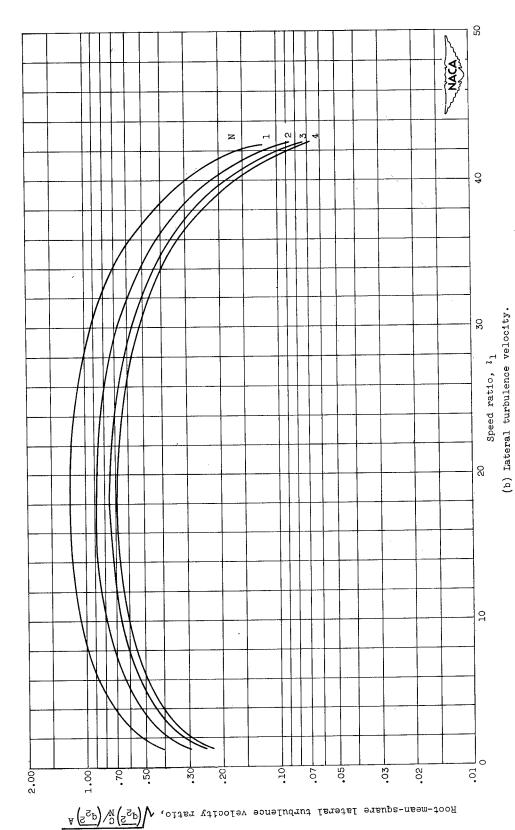


Figure 5. - Concluded. Effect of multiple screens N and speed ratio (M_B of 0.05) on root-mean-square turbulence velocity ratio in absence of turbulence decay for screen-axisymmetric-contraction configurations with upstream isotropic turbulence and constant screen losses. Over-all screen pressure-drop coefficient, NK, 6.

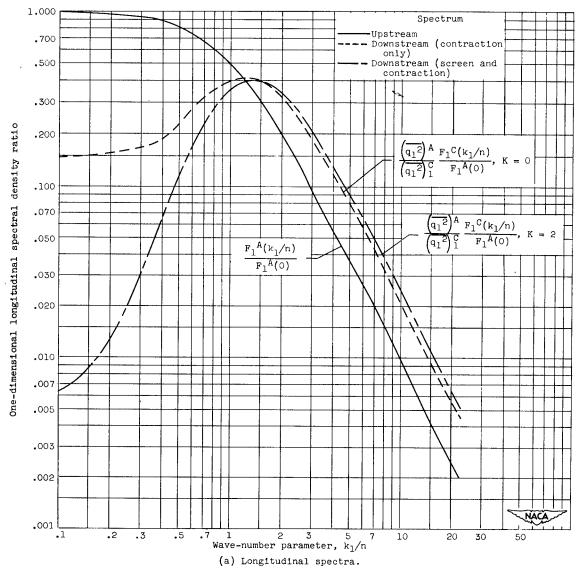


Figure 6. - Comparison of one-dimensional spectra in absence of turbulence decay for contraction and for single-screen-contraction configurations for upstream isotropic turbulence having amplitude function $G(k) = H(k^2 + n^2)^{-3}$. M_B, 0.05; M_C, 2.00; \imath_1 , 29.822.

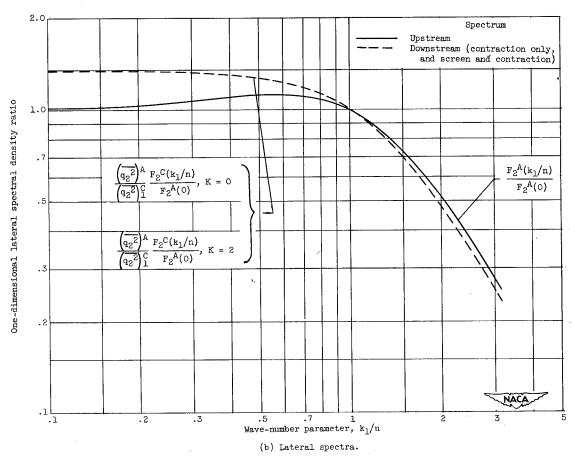


Figure 6. - Concluded. Comparison of one-dimensional spectra in absence of turbulence decay for contraction and for single-screen-contraction configurations for upstream isotropic turbulence having amplitude function $G(k) = H(k^2 + n^2)^{-3}$. M_B , 0.05; M_C , 2.00; l_1 , 29.822.

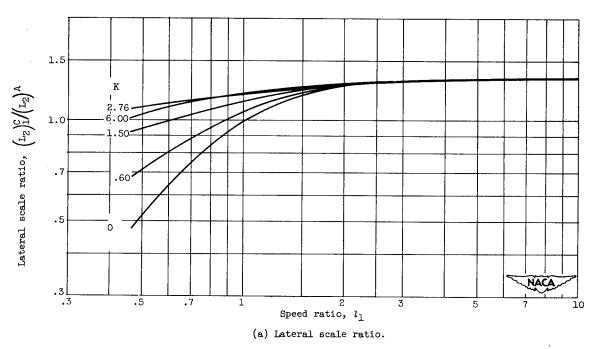
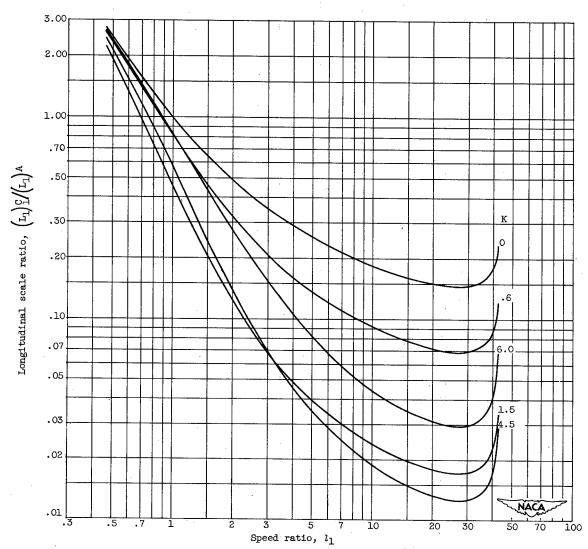


Figure 7. - Variation of scale ratio with speed ratio ($M_{
m B}$ of 0.05) and screen pressure-drop coefficient K in absence of turbulence decay for single-screen-axisymmetric-contraction configurations with upstream isotropic turbulence.



(b) Longitudinal scale ratio. Longitudinal scale ratio equals zero for $\,$ K $\,\thickapprox\,$ 2.76.

Figure 7. - Concluded. Variation of scale ratio with speed ratio ($M_{\rm B}$ of 0.05) and screen pressure-drop coefficient K in absence of turbulence decay for single-screen-axisymmetric-contraction configurations with upstream isotropic turbulence.

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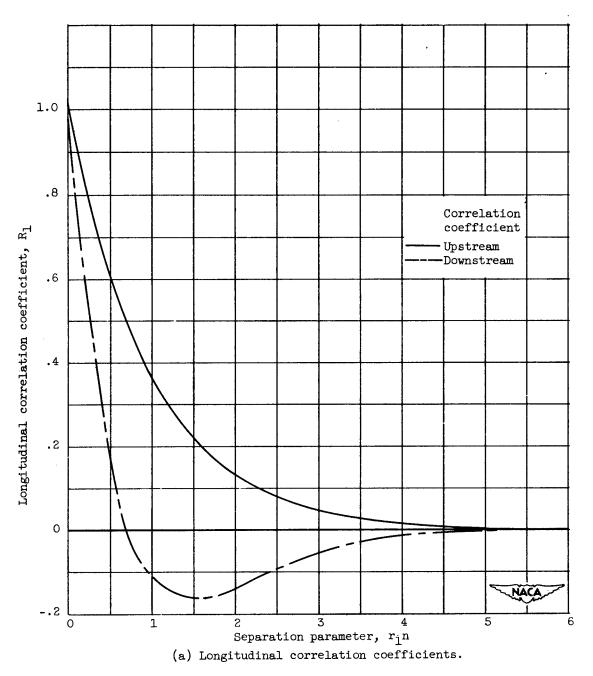


Figure 8. - Comparison of correlation coefficients in absence of decay for a screen-contraction configuration ($M_B = 0.05$, $M_C = 2.00$, K = 2, N = 1) with upstream isotropic turbulence having amplitude function $G(k) = H(k^2 + n^2)^{-3}$.

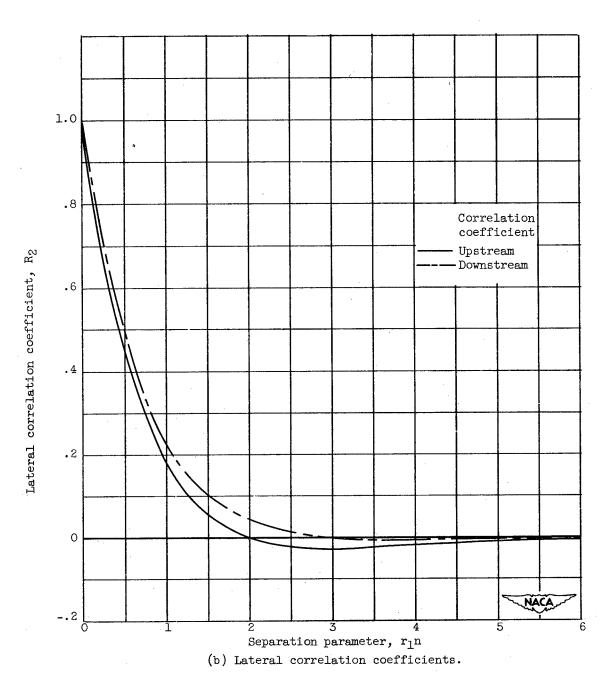


Figure 8. - Concluded. Comparison of correlation coefficients in absence of decay for a screen-contraction configuration (M_B = 0.05, M_C = 2.00, K = 2, N = 1) with upstream isotropic turbulence having amplitude function $G(k) = H(k^2 + n^2)^{-3}$.

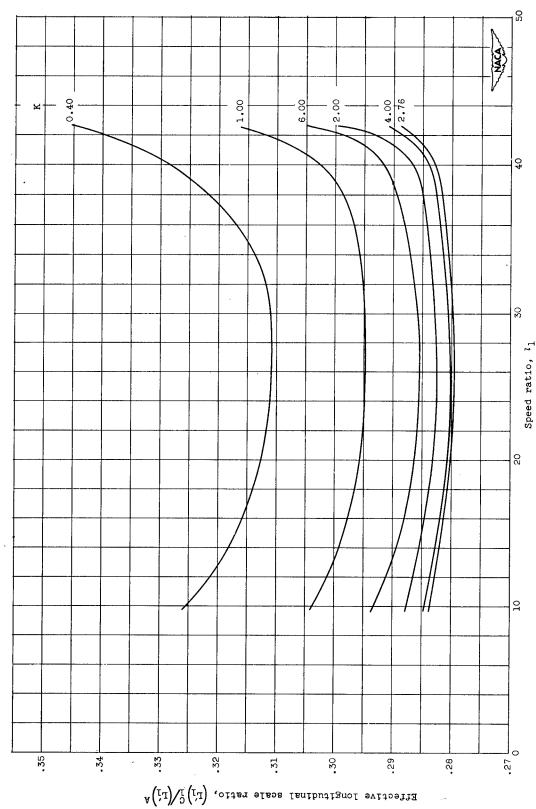


Figure 9. - Variation of effective longitudinal scale ratio in absence of turbulence decay with speed ratio ($M_{\rm B}$ of 0.05) and screen pressure-drop coefficient K for single-screen-axisymmetric-contraction configuration with upstream isotropic turbulence having amplitude function $G(k) = H(k^2 + n^2)^{-3}$.

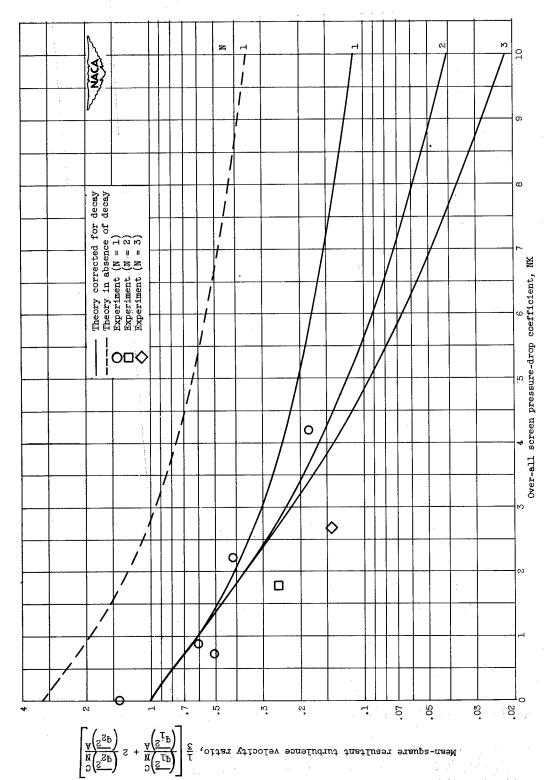


Figure 10. - Comparison of theoretical mean-square resultant turbulence velocity ratios corrected for decay with experiment of reference 1. Speed ratio l_1 , 6.7 ($M_{\rm B}$ = 0.05, $M_{\rm C}$ = 0.34); N screens in series; upstream isotropic turbulence; scale $L_{\rm C}^2$, 0.05 foot (estimated).

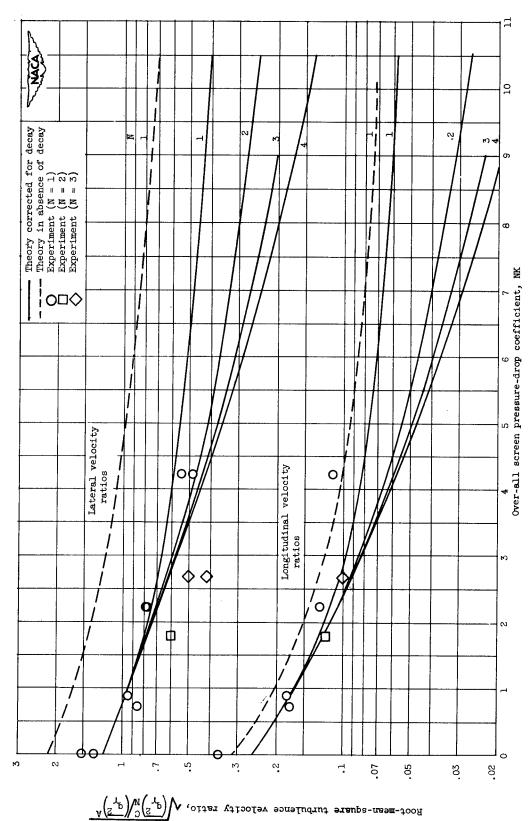


Figure 11. - Comparison of theoretical root-mean-square longitudinal and lateral turbulence velocity ratios corrected for decay with experiment of reference 1. Speed ratio l_1 , 6.7 ($M_{\rm B}$ = 0.05, $M_{\rm C}$ = 0.34); N screens in series; upstream isotropic turbulence; scale L_2^A , 0.05 foot (estimated).